

WAVES IN THE ION CYCLOTRON FREQUENCY RANGE AT EARTH AND MERCURY



Eun-Hwa Kim

Princeton Plasma Physics Laboratory

In collaboration with

Jay Johnson

Scott Boardsen

James Slavin

Dong-Hun Lee

Hyomin Kim

Princeton Plasma Physics Laboratory

NASA/GSFC, University of Maryland

University of Michigan

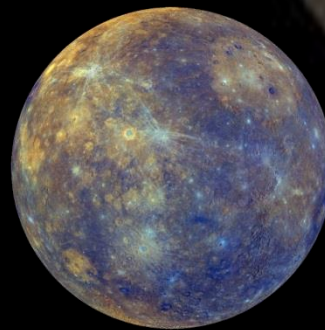
Kyung Hee University, Korea

New Jersey Institute of Technology

Laboratory plasmas

Shot number : 1216
Frame Count : 042
2008/07/15 11:39:19

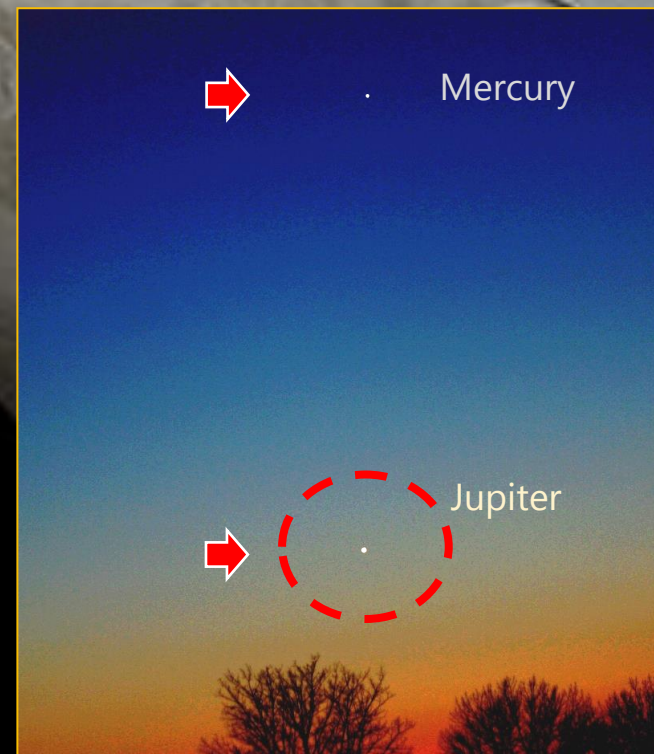
KSTAR TU02



Mercury



Mercury



Laboratory plasmas

Shot number : 1216
Frame Count : 042
2008/07/15 11:39:19

KSTAR TU02

Earth

Jupiter

Mercury

$$f \sim f_{ci}$$

Laboratory plasmas

Shot number : 1216
Frame Count : 042
2008/07/15 11:39:19

KSTAR TU02

Jupiter

$$f \sim f_{ci}$$

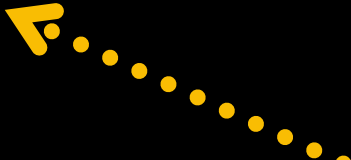
Earth

Mercury

Ion-Ion Hybrid
Resonance !

@ Mercury

- What are the **observed ULF waves**? How can they propagate to higher magnetic latitude?



Mode-converted
waves
at the Ion-ion hybrid
resonance

@ Earth

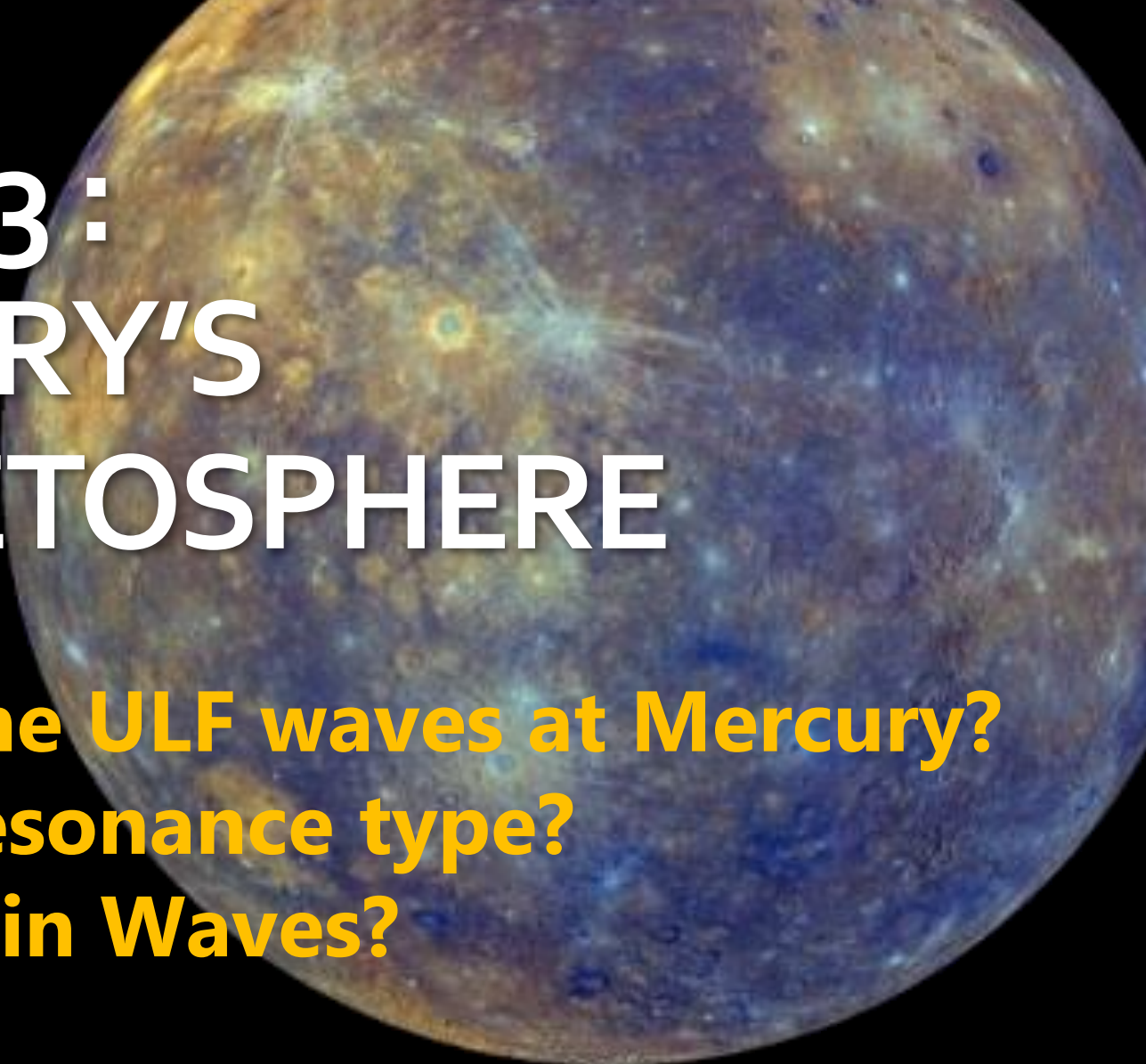
- How are **linearly polarized EMIC waves** generated?

@ Mercury & Earth

- Can we use the **detected waves** as a diagnostic tool to estimate **heavy ion density**?



Application!



PART 1/3 : MERCURY'S MAGNETOSPHERE

**What are the ULF waves at Mercury?
Field line resonance type?
Ion Bernstein Waves?
or ?**

Mercury's magnetosphere

Magnetosphere

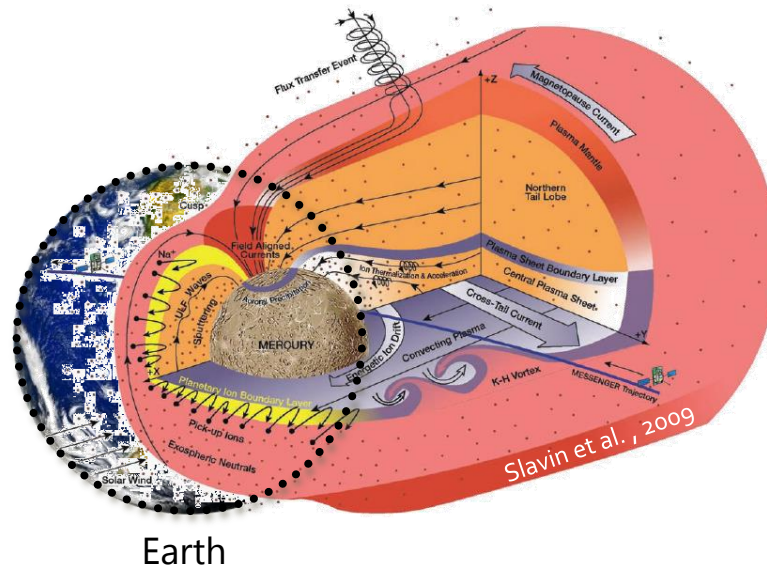
- + No atmosphere
- + No ionosphere
- + No plasmasphere
- + No co-rotational electric field to trap cold plasma
- + Na exosphere

Plasma conditions

- + Multi-ion
 - H, He from Sun
 - heavy ions
 - : sputtered from surface and ionized
- + Hot plasma

Dimension

- + Small magnetosphere
 - : sub-solar point $\sim 1.4 R_M$
- + $1.34 R_M \sim 10.8 R_E$



Earth

Mercury's magnetosphere

Magnetosphere

- + No atmosphere
- + No ionosphere
- + No plasmasphere
- + No co-rotational electric field to trap cold plasma
- + Na exosphere

Plasma conditions

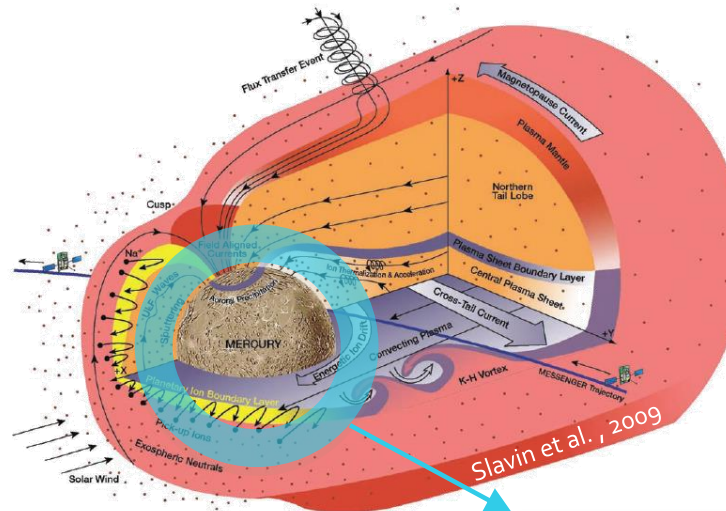
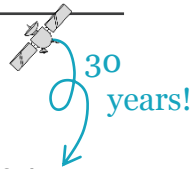
- + Multi-ion
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- + Hot plasma

Dimension

- + Small magnetosphere
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- + $1.34 R_M \sim 10.8 R_E$

Missions

- + Mariner 10, 1973
 - three flybys
- + MESSENGER, 2004
 - three flybys
 - orbit, 2011 (period 8hrs, 2012 ~)
 - Magnetometer (20 samples/s)
 - No electric field measurement



ULF wave observation

Compressional dominant (75%)

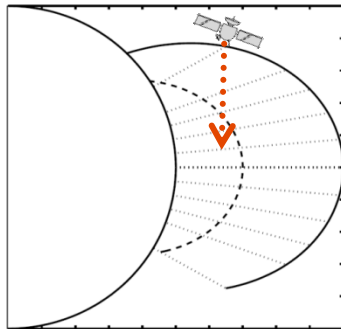


Transverse dominant (25%)

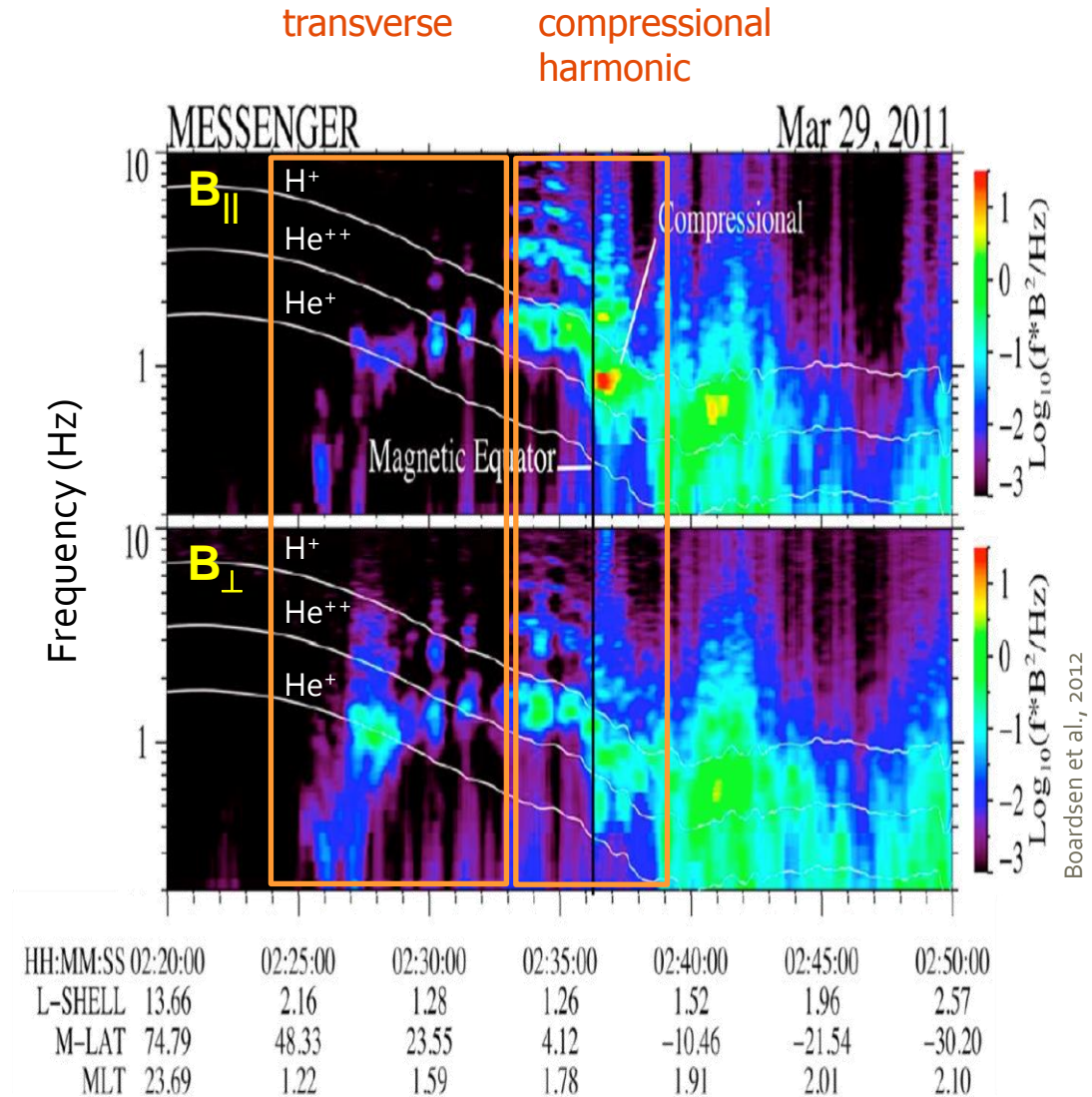
ULF waves at Mercury

MESSENGER

- + Frequency
 - $f_{\text{He}} < f < f_{\text{H}}$
- + M-LAT : $-5^\circ \sim 45^\circ$
MLT : 1.3 h \sim 1.7 h

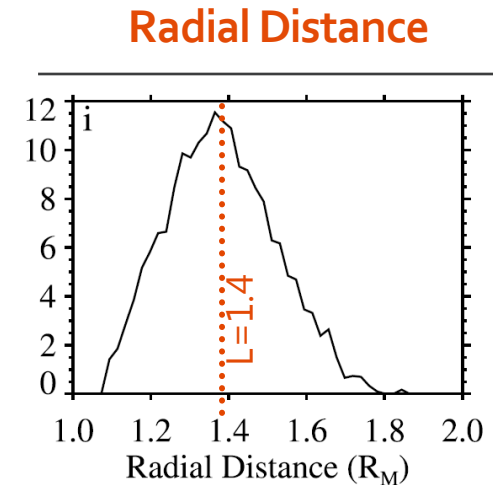
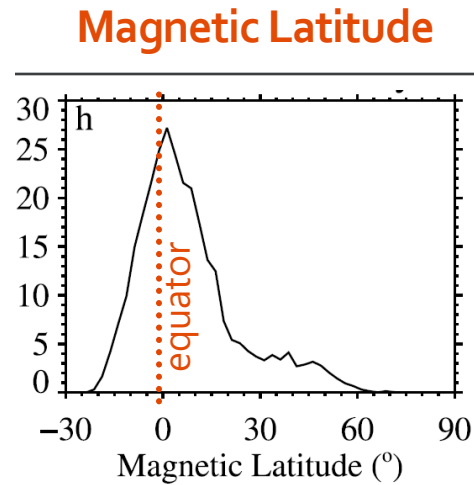
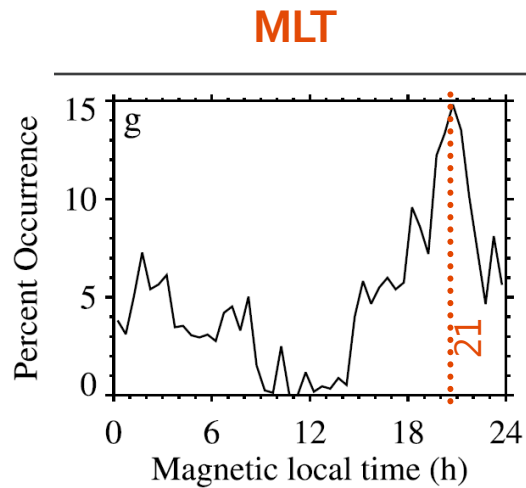


- + Equator
 - compressional
 - harmonic
- + Off Equator
 - transverse

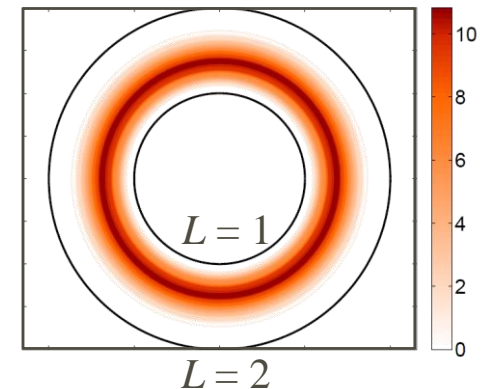
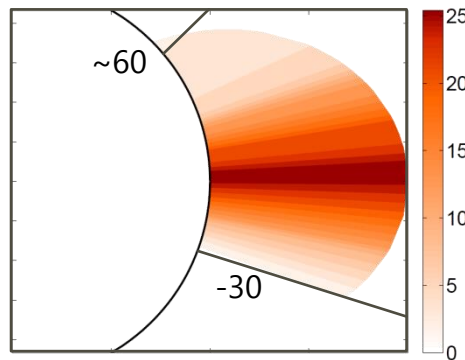
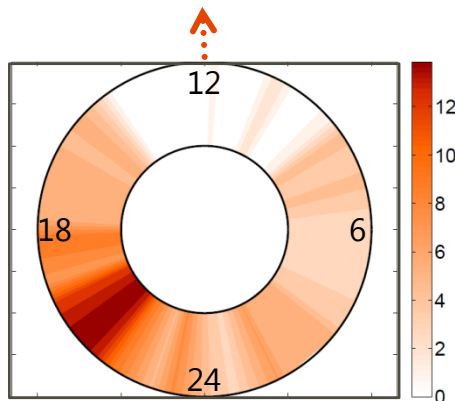


Statistical Study using MESSENGER

: Percent Occurrence (3/24/11 ~ 09/25/11 : 2.1 Mercury Year)



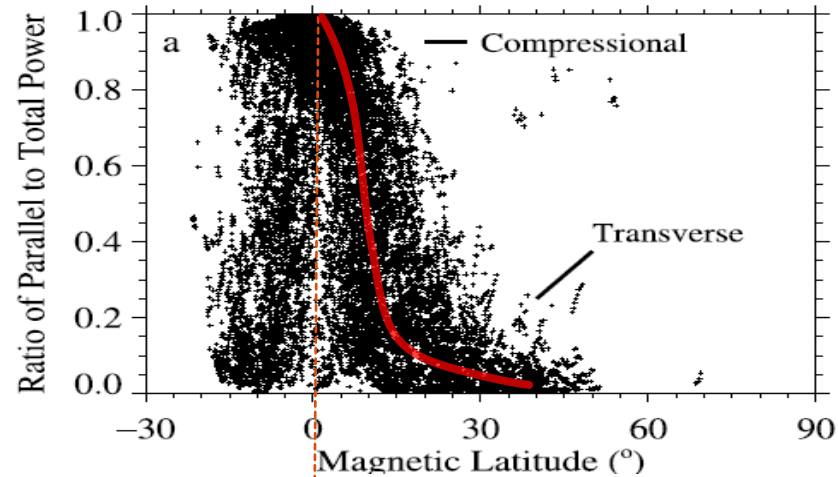
Sunward



Polarization along magnetic latitude

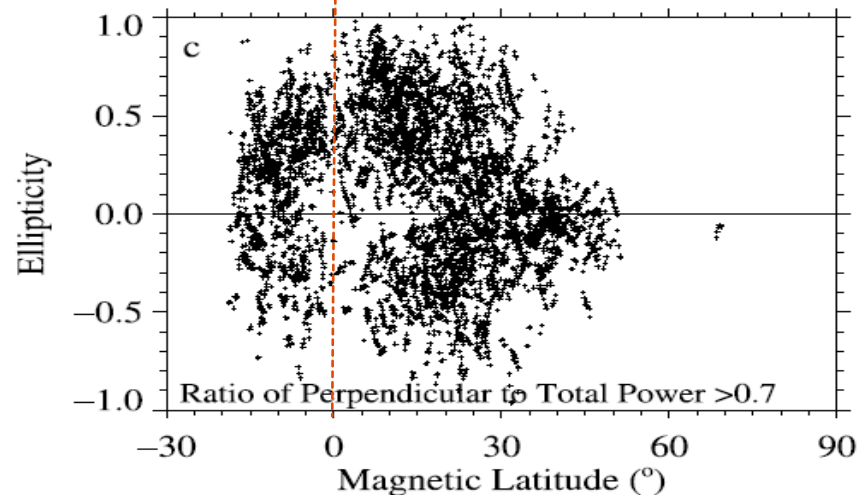
Ratio of Parallel to Total Power

- + Off Equator
→ compressional
- + Equator
→ Transverse



Ellipticity

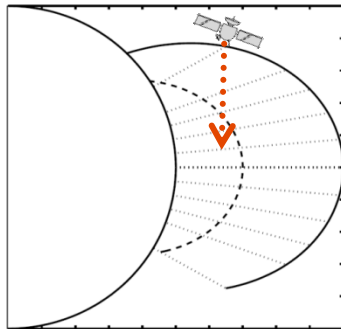
- + Off Equator
→ linear
- + Equator
→ circular / mixed



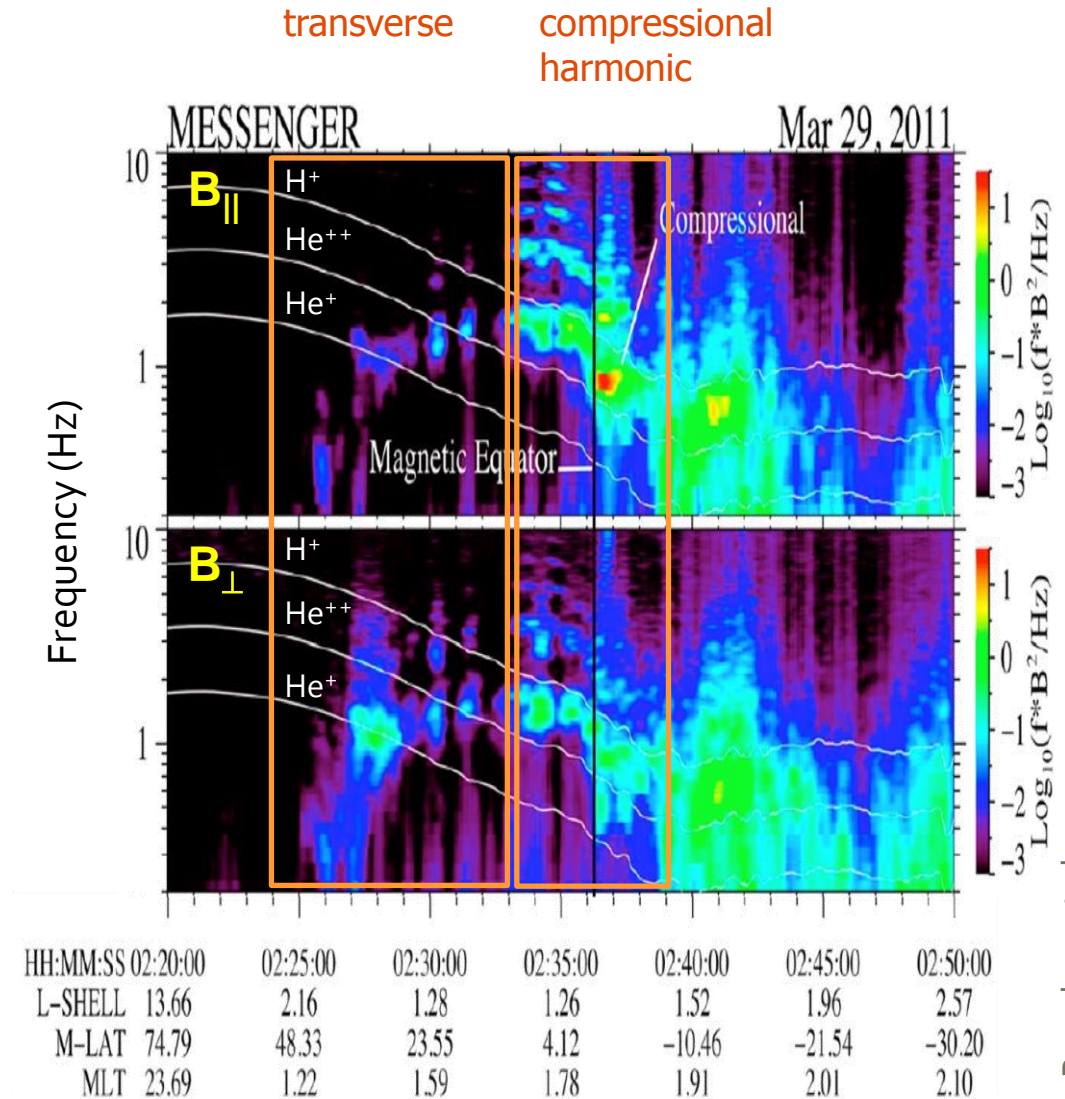
ULF waves at Mercury

MESSENGER

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MLT : 1.3 h \sim 1.7 h



- + Equator
 - compressional
 - harmonic
- + Off Equator
 - transverse



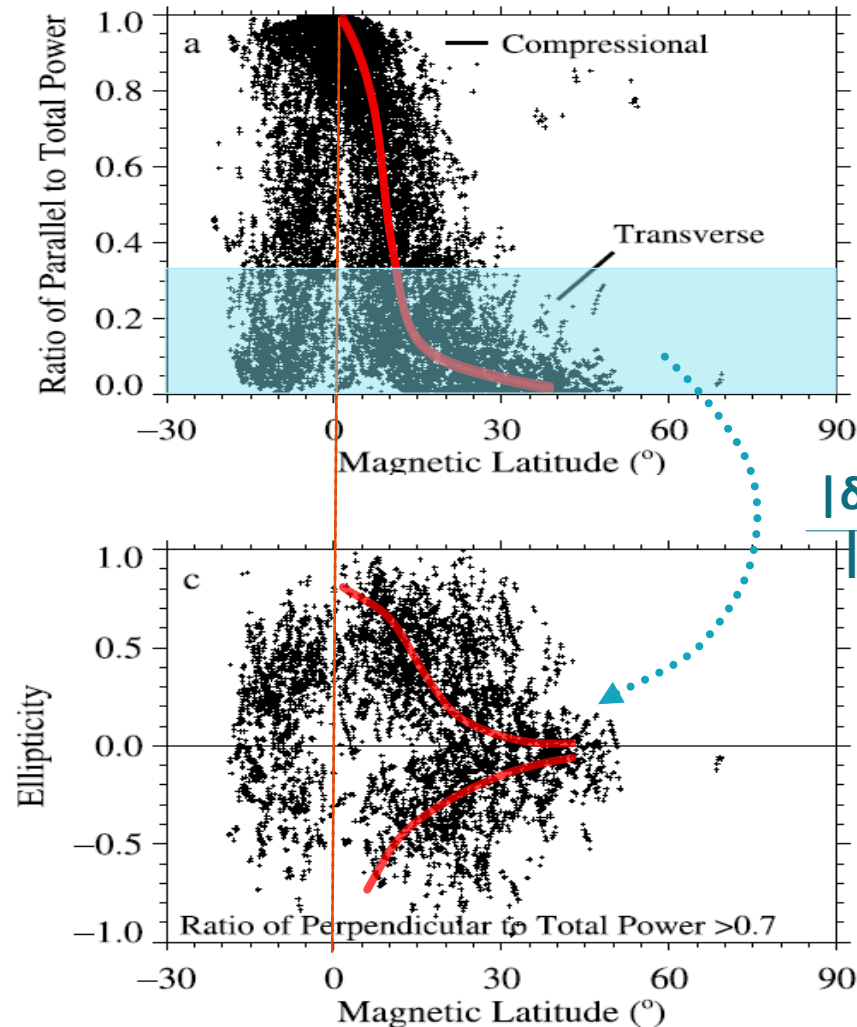
Polarization along magnetic latitude

Ratio of Parallel to Total Power

- + Off Equator
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Ellipticity

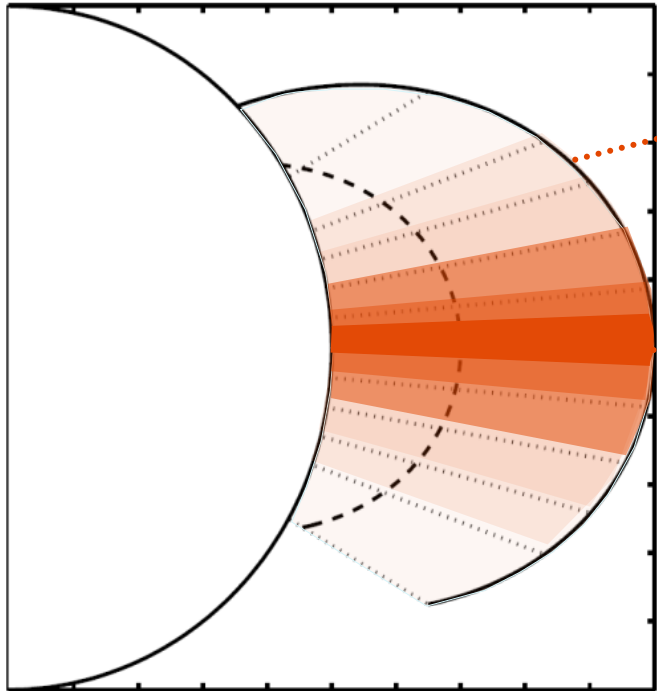
- + Off Equator
→ linear
- + Equator
→ circular / mixed



$$\frac{|\delta b_{\perp}|^2}{|b|^2} > 0.7$$

Summary

: Wave Characteristics



off Equator

Weak occurrence
Transverse and Linear

Equator

High occurrence
Compression and Harmonic

Ion-ion hybrid resonance

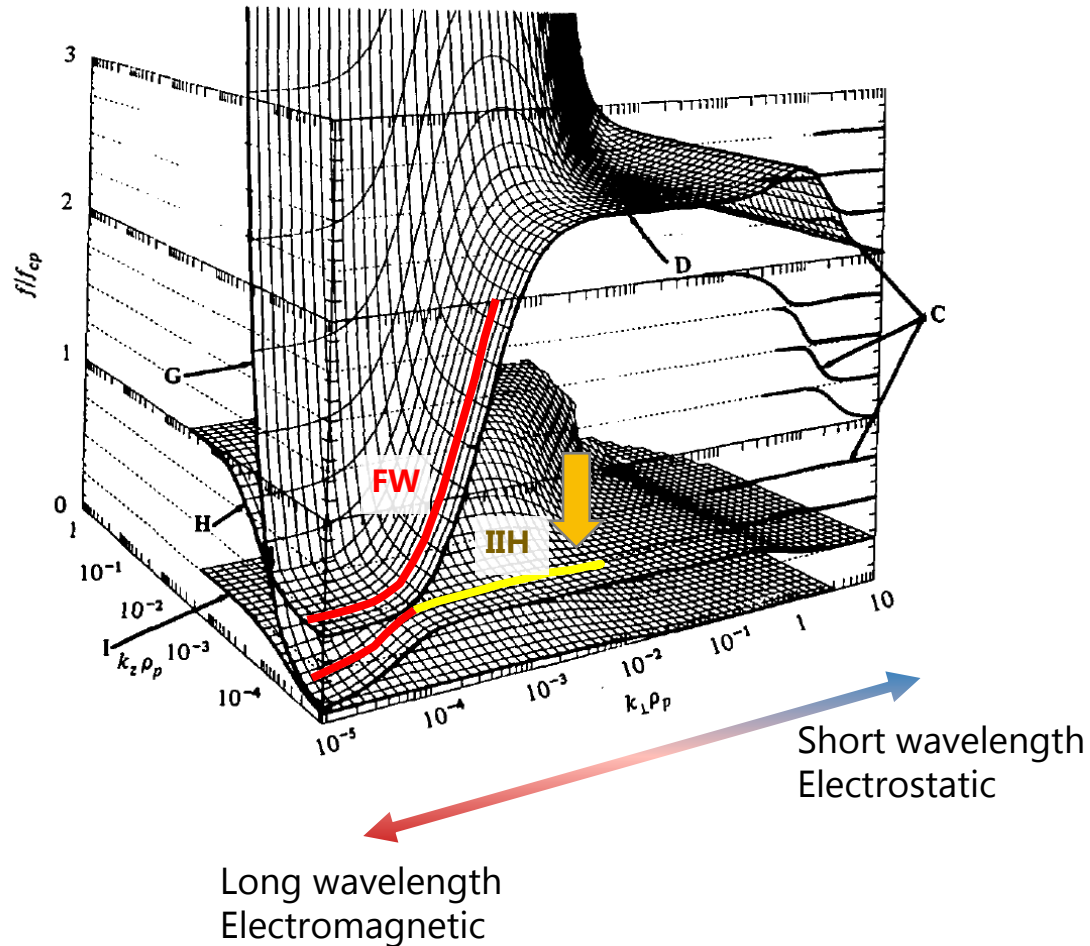
between two ion gyrofrequencies

- + Fast compressional waves are converted to "ion-ion hybrid resonance"
- + Mode converted ion-ion hybrid resonance
 - Field-aligned propagation
 - Long wavelength in field-aligned direction
 - $k_{\perp} \gg k_{\parallel}$
 - Transverse waves
 - Linear polarization

→ 2D Full wave calculations has been performed in Mercury's magnetosphere

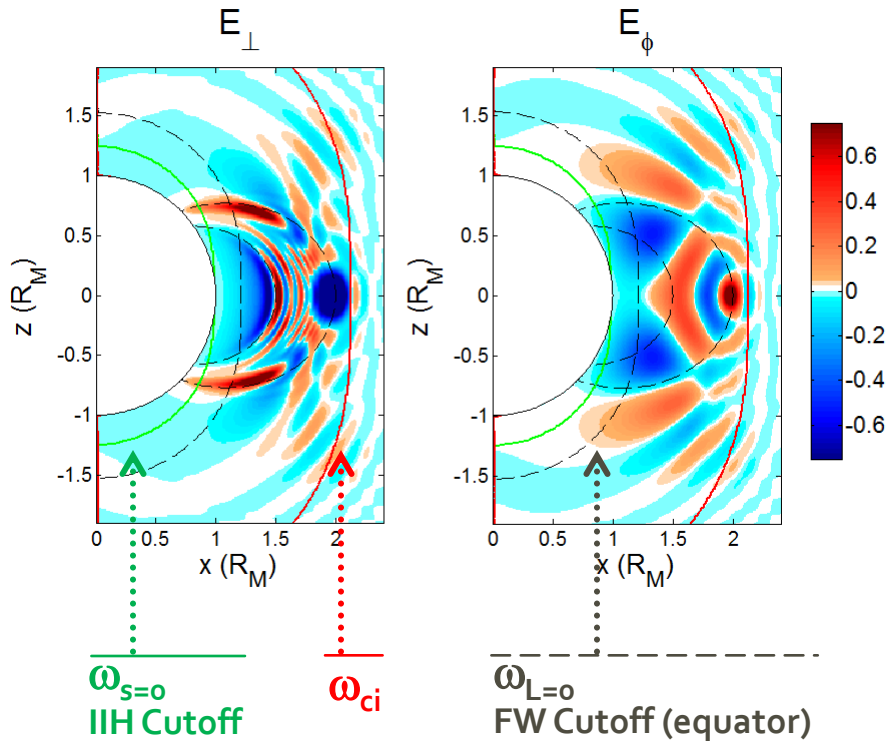
FW : Fast compressional wave

IIH : Mode-converted Ion-ion hybrid resonant wave



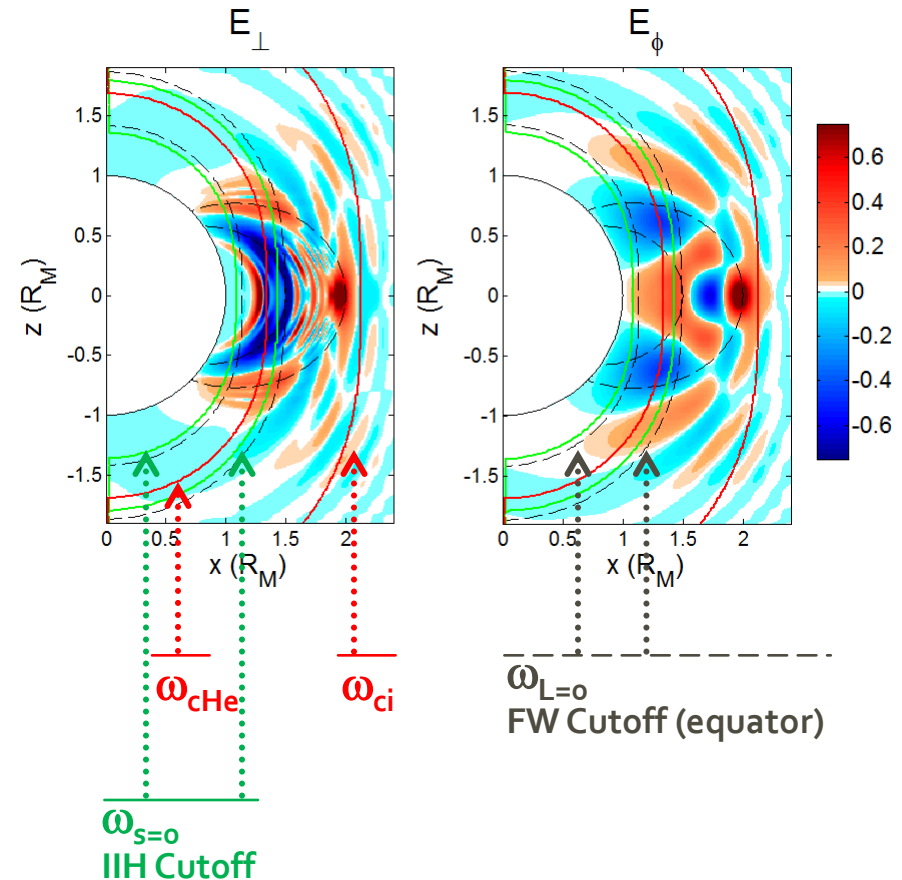
Full wave calculations (cold)

H⁺ 85% Na⁺ 15%



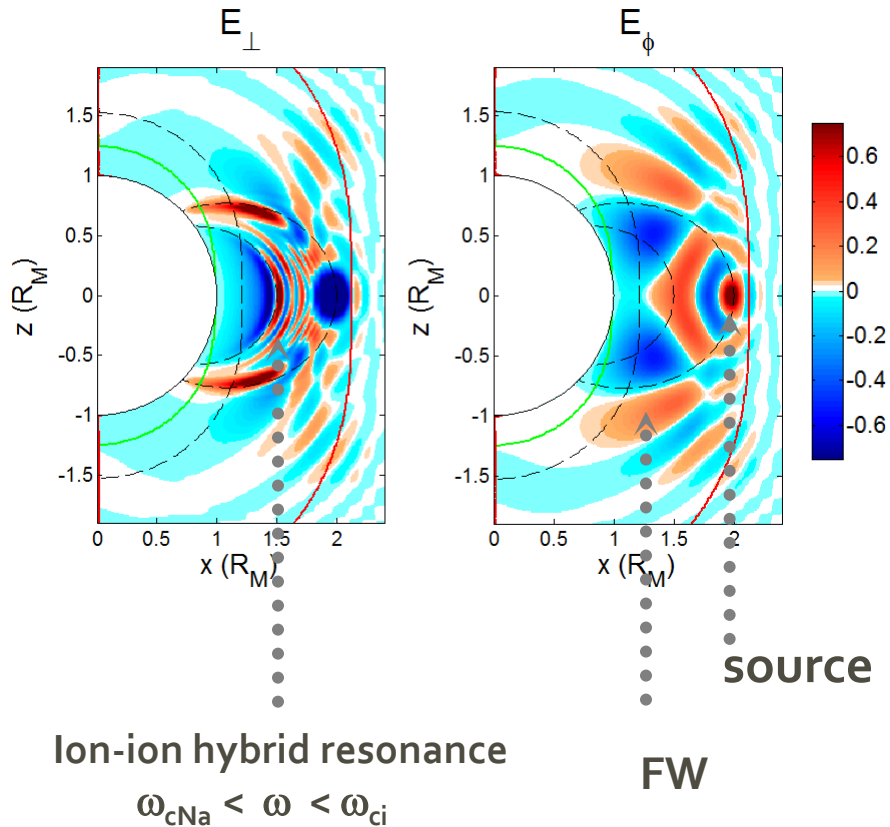
- + B_0 (surface) : 3×10^{-7} T
- + N_e : $3 / \text{cm}^3$
- + $f = 0.8 f_{ci}$ at $L=2$ (equator)

H⁺ 85% He⁺ 7.5% Na⁺ 7.5%

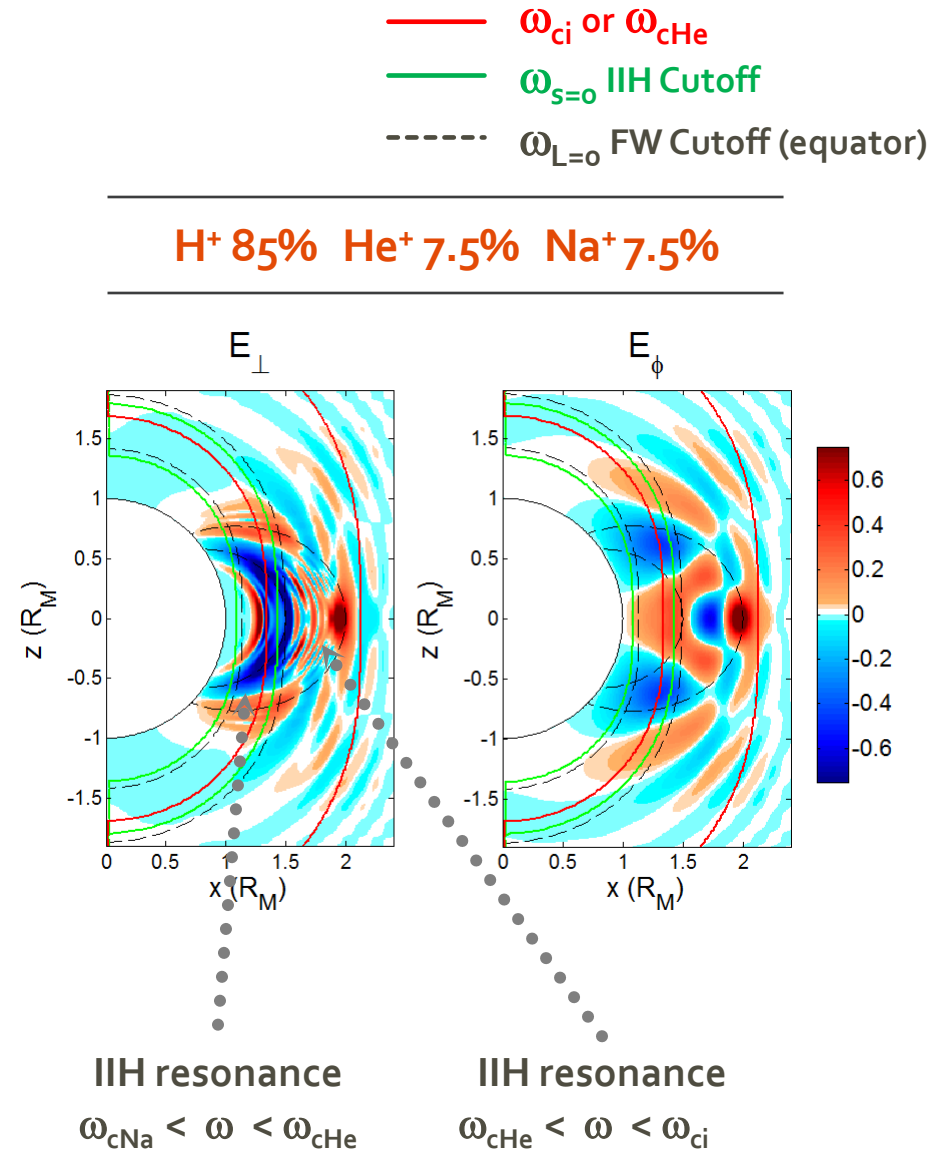


Full wave calculations

H⁺ 85% Na⁺ 15%



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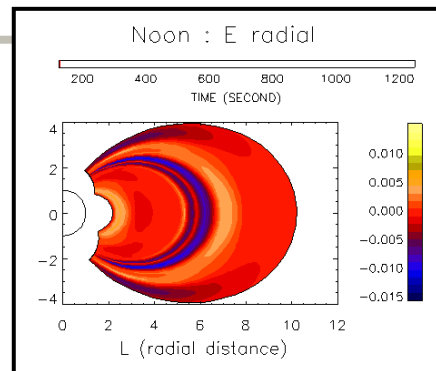
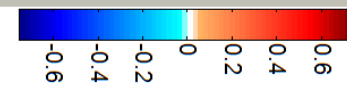
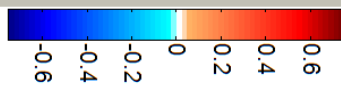
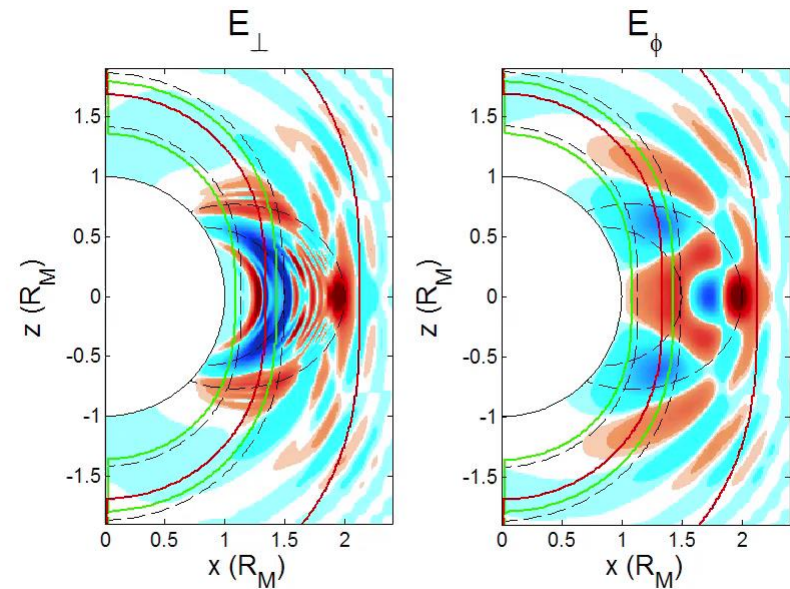
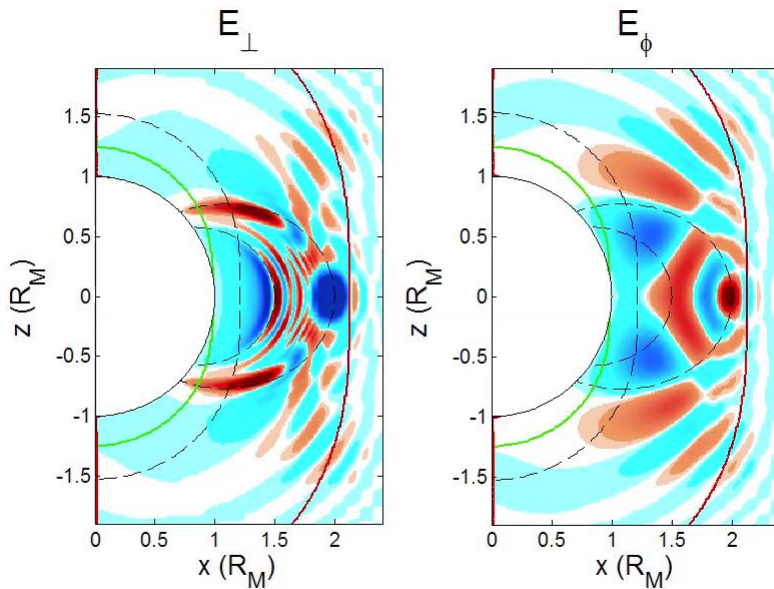


Full wave calculations

- ω_{ci} or ω_{cHe}
- $\omega_{s=0}$ LH Cutoff
- - - $\omega_{L=0}$ FW Cutoff (equator)

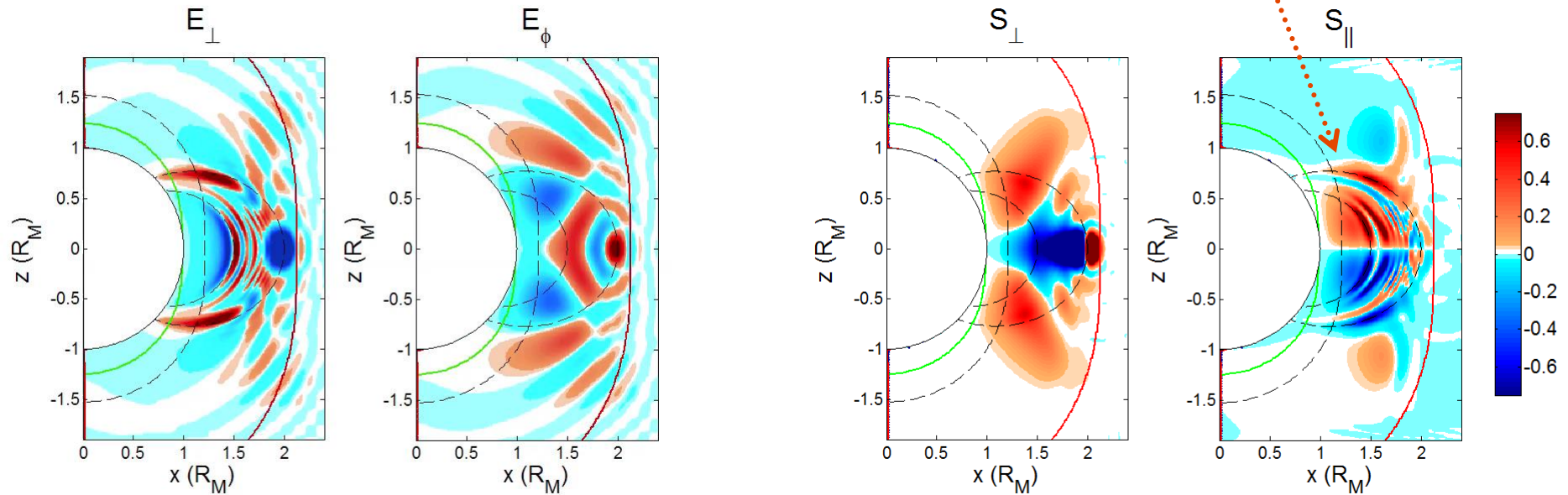
H^+ 85% Na^+ 15%

H^+ 85% He^+ 7.5% Na^+ 7.5%

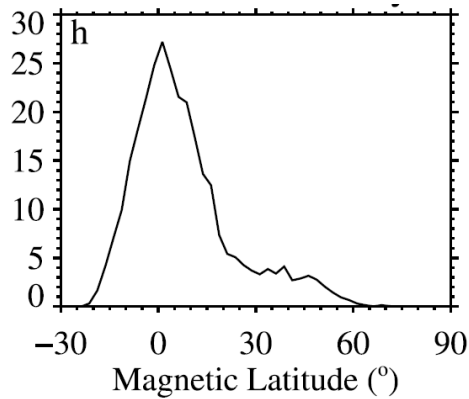
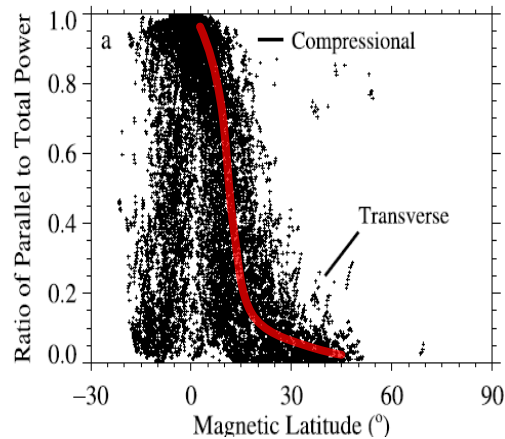


Poynting Flux

H^+ 85% Na^+ 15%

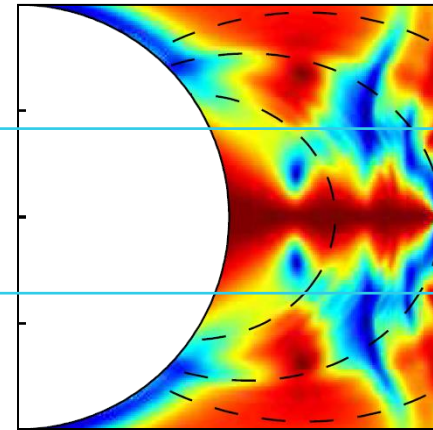
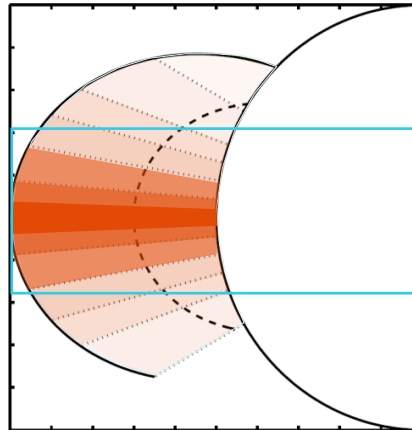


Comparison with observation



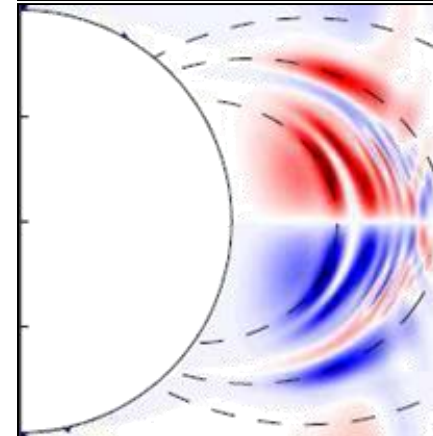
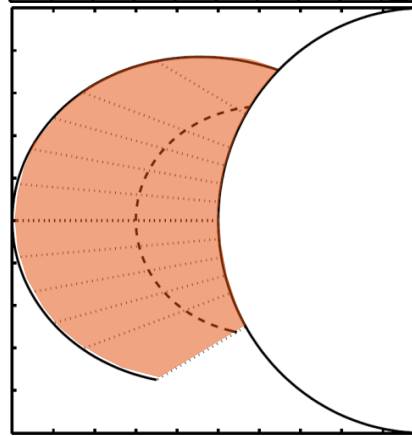
Observation

Full wave calculation



Compressibility

Equator - high
Off Equator - low



Latitude
coverage

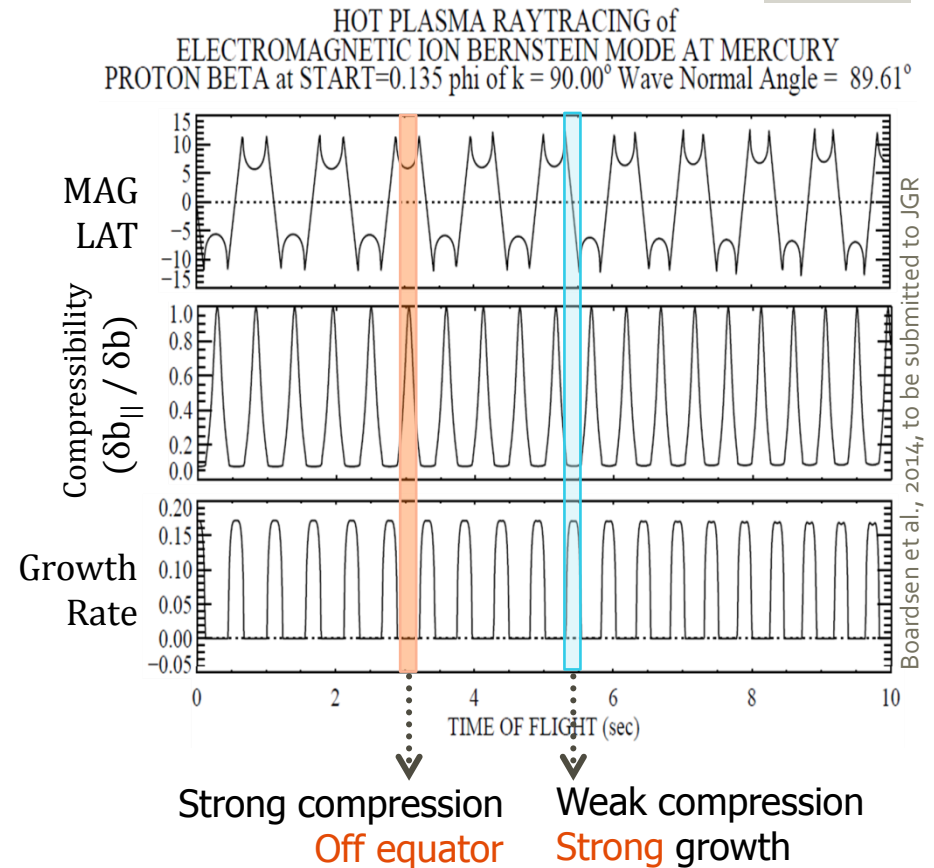
cf. Ion Bernstein Waves : Ray Tracing

Type A

$$\beta = 0.135$$

- + **Ray tracing**
 - bi-modal structure
 - Weak compression and strong growth near equator
 - Highly compression near $|4^\circ - 7^\circ|$
- + $\beta = 0.051$
 - also shows only Type A

*It could explain MESSENGER
because it occurs in various
beta range.*



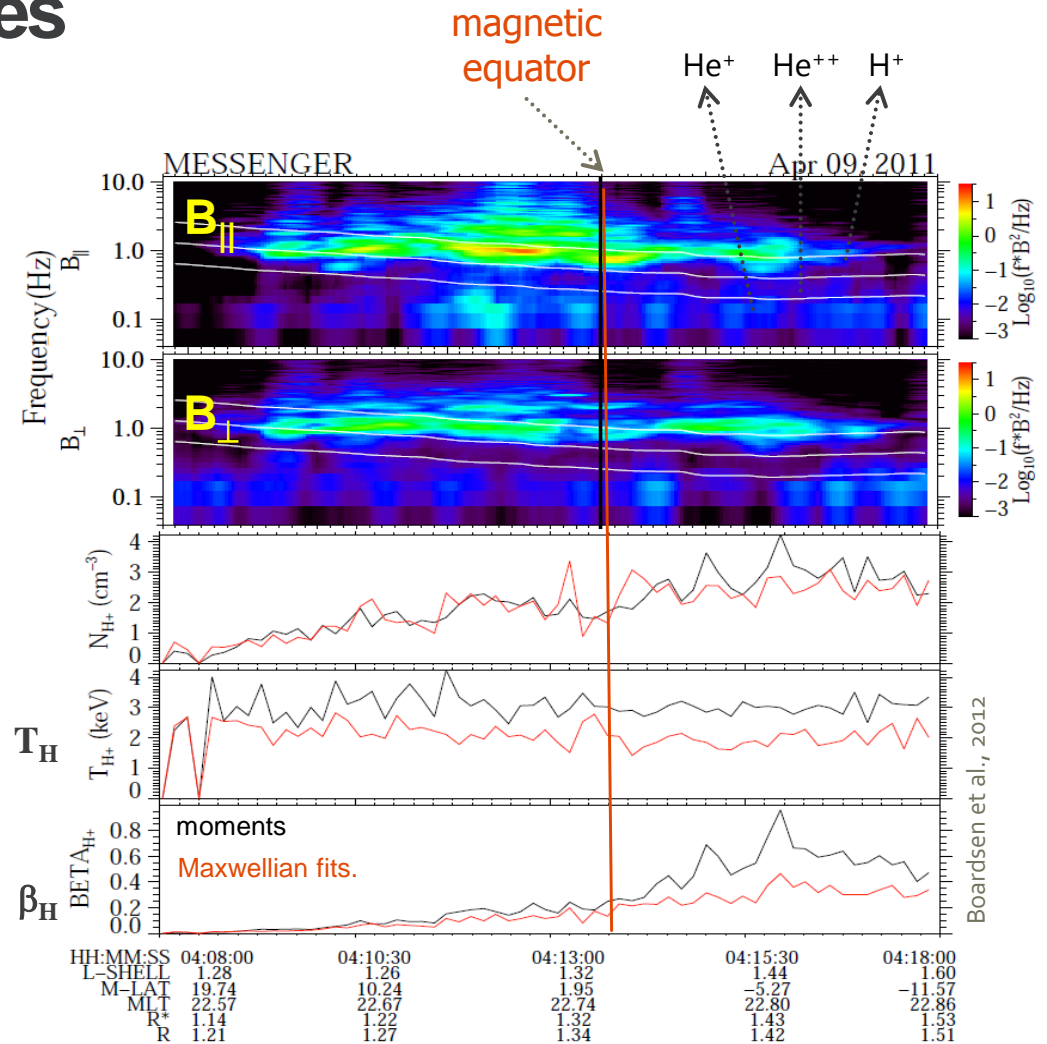
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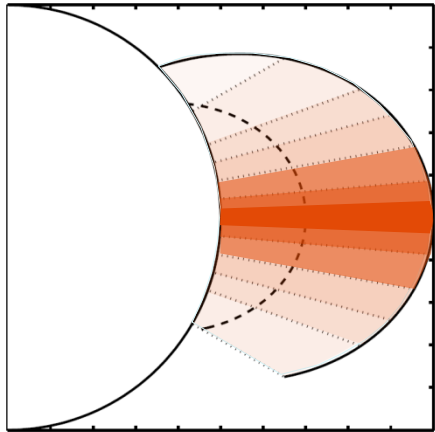
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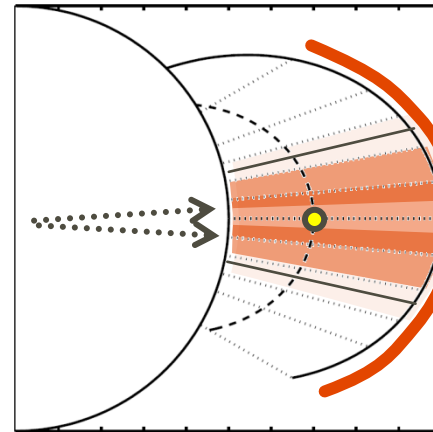
cf. Ion Bernstein Waves : Comparison with observation

Observation



Highly
Compression
near Equator

Ray tracing



Observation

Ray Tracing

Comparison

Full wave calculations

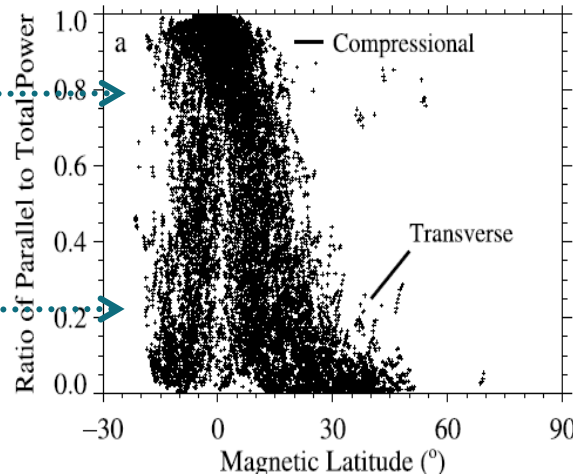
Observation

IBW ray tracing

Compressional
Wave power ?

Ion Bernstein waves

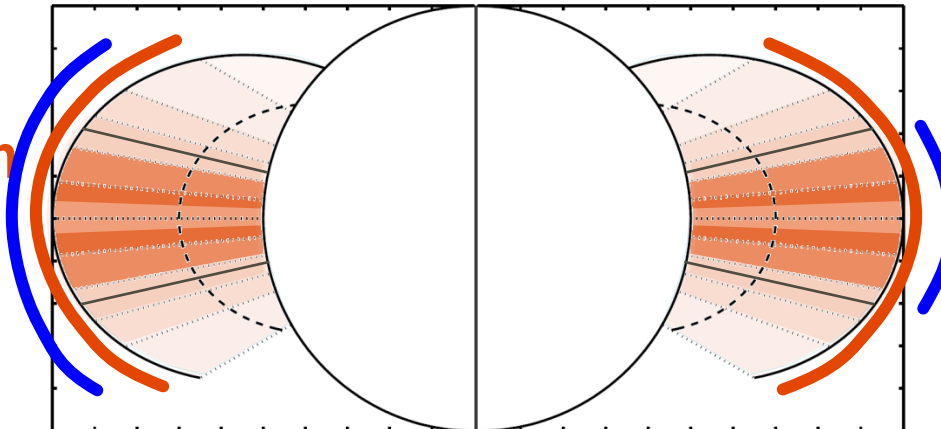
Long-wave length
Mode-converted
waves



COLD plasma

Doppler Shift

Observation
FLR



Observation
Ray Tracing

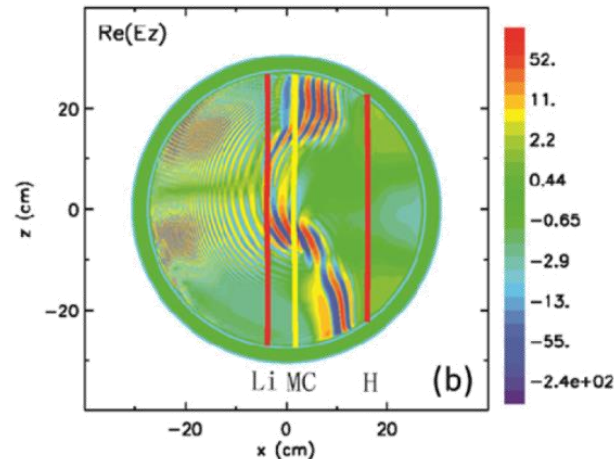
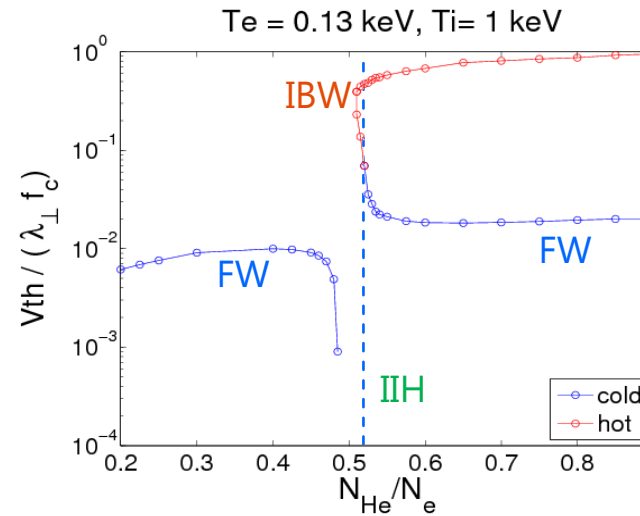
Mode Conversion in hot plasma

FW : Fast compressional wave
 IIH : Mode-converted ion-ion hybrid resonant wave
 IBW : Ion Bernstein waves

Dispersion relation at Mercury

- + using WHAMP
- + Parameters
 - $B_0 = 90$ nT
 - $N_e = 3$ cm $^{-3}$
 - $K_{||} = 2\pi/(1.5R_M)$
 - $T_{\perp}/T_{||} = 1$
 - $T_{ion} = 1$ keV
 - $T_e = 0.13$ keV
 - $\omega = 0.7 \omega_{ci}$
 - No cold plasma

- + At Mercury's hot plasmas, mode conversion from **fast compressional waves** to **ion-Bernstein waves** occurs at the ion-ion hybrid resonance
 ← Similar to laboratory plasma





PART 2: EARTH'S MAGNETOSPHERE

**Linear Polarization
EMIC waves
& IIH resonance**

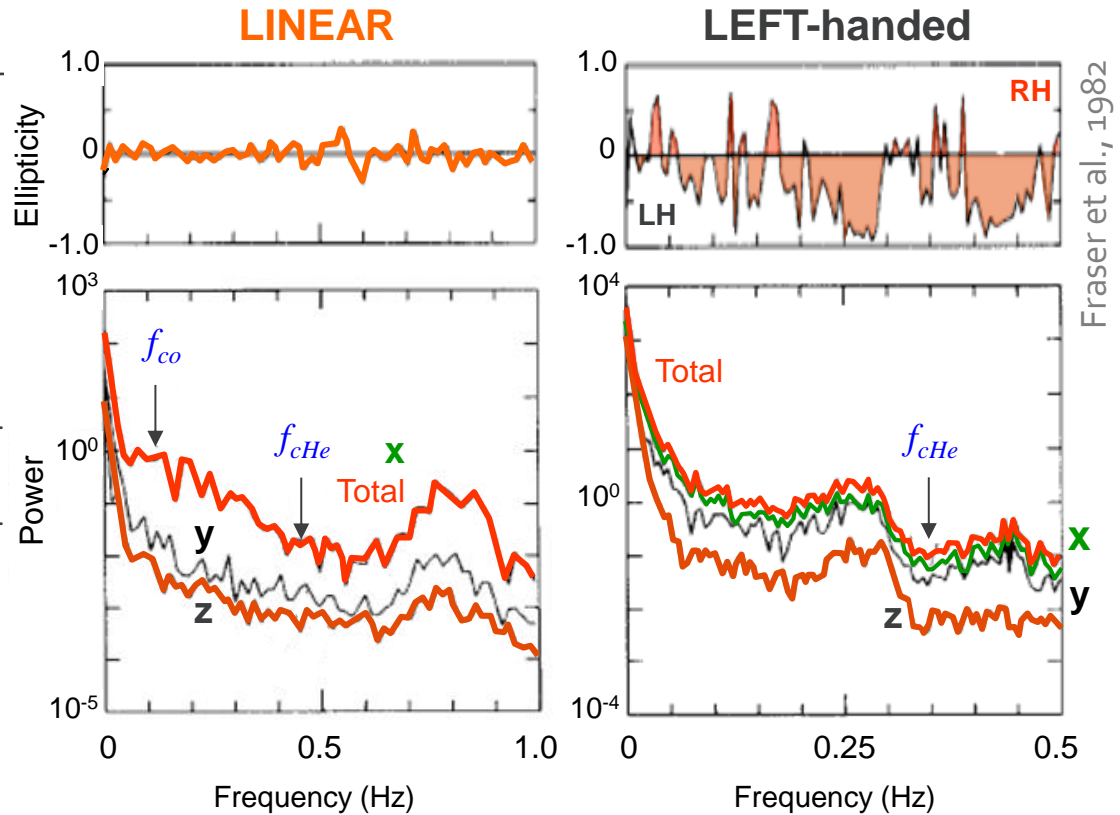
EMIC waves at Earth

Left-handed Polarization

+ Ion cyclotron instability by proton temperature anisotropic

Linear Polarization

+ mode conversion at the IHH resonance [Lee et al., 2008]



EMIC waves at Earth

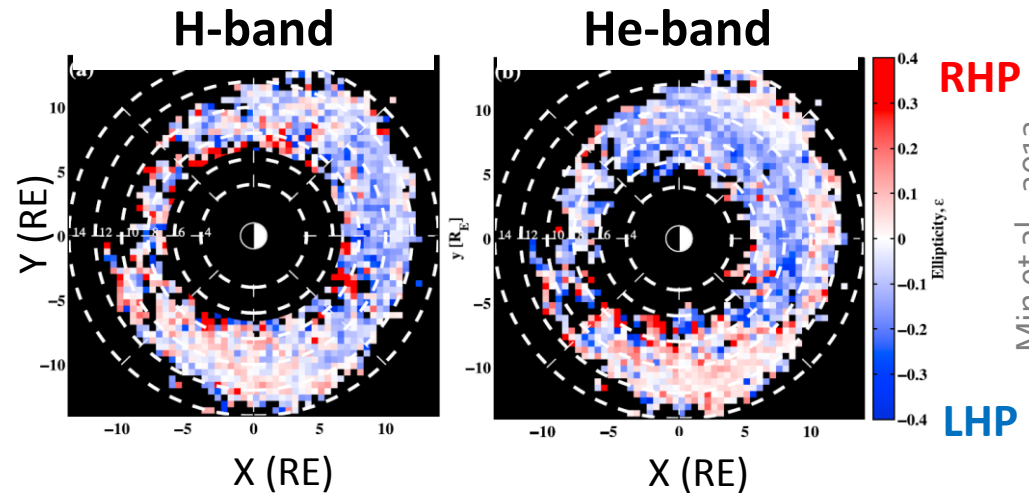
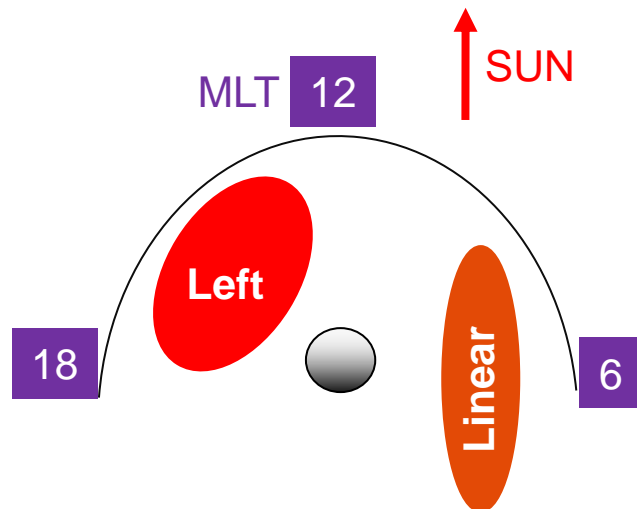
Linear Polarization

+ Linearly Polarized EMIC waves are observed in a wide range of L-shell

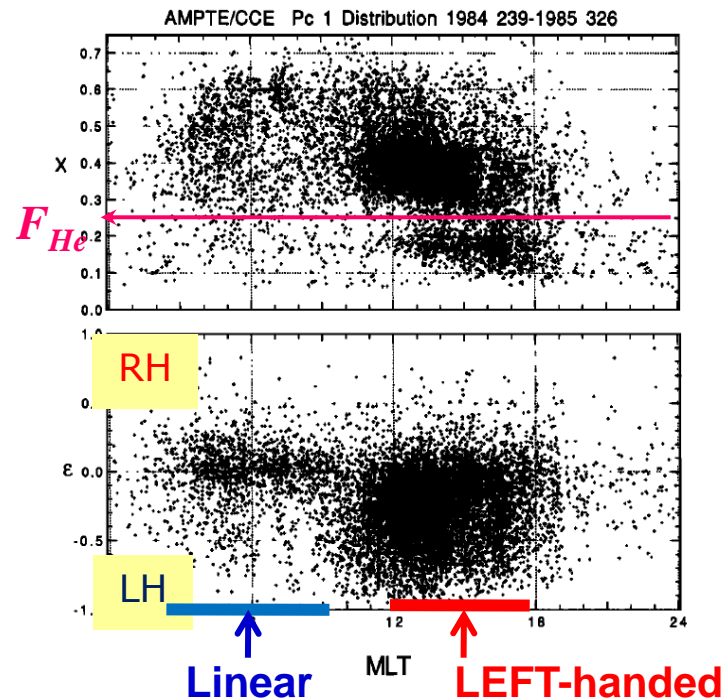
Issue:

How linear polarization is dominant?

How such EMIC waves can be generated?



Min et al., 2012

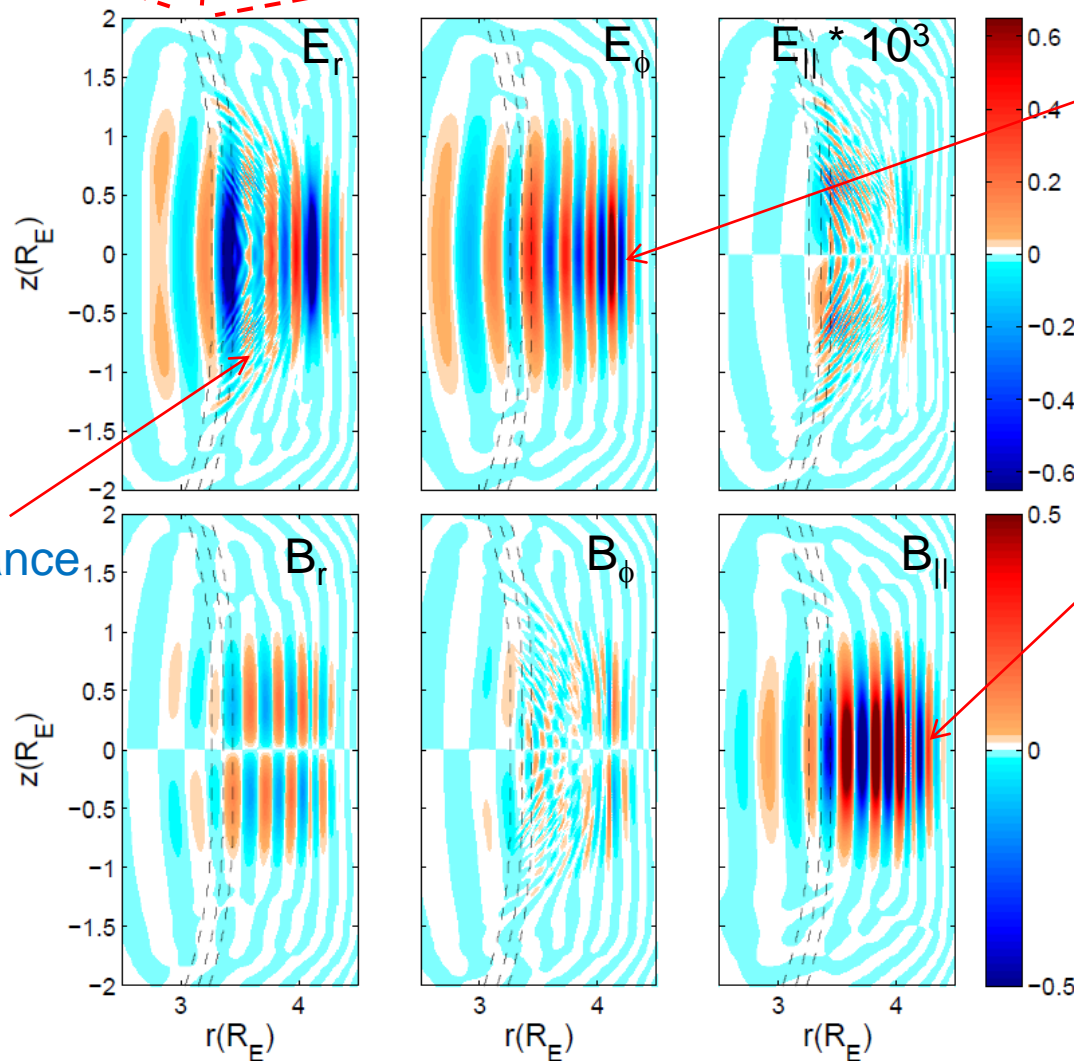


Anderson et al., 1992

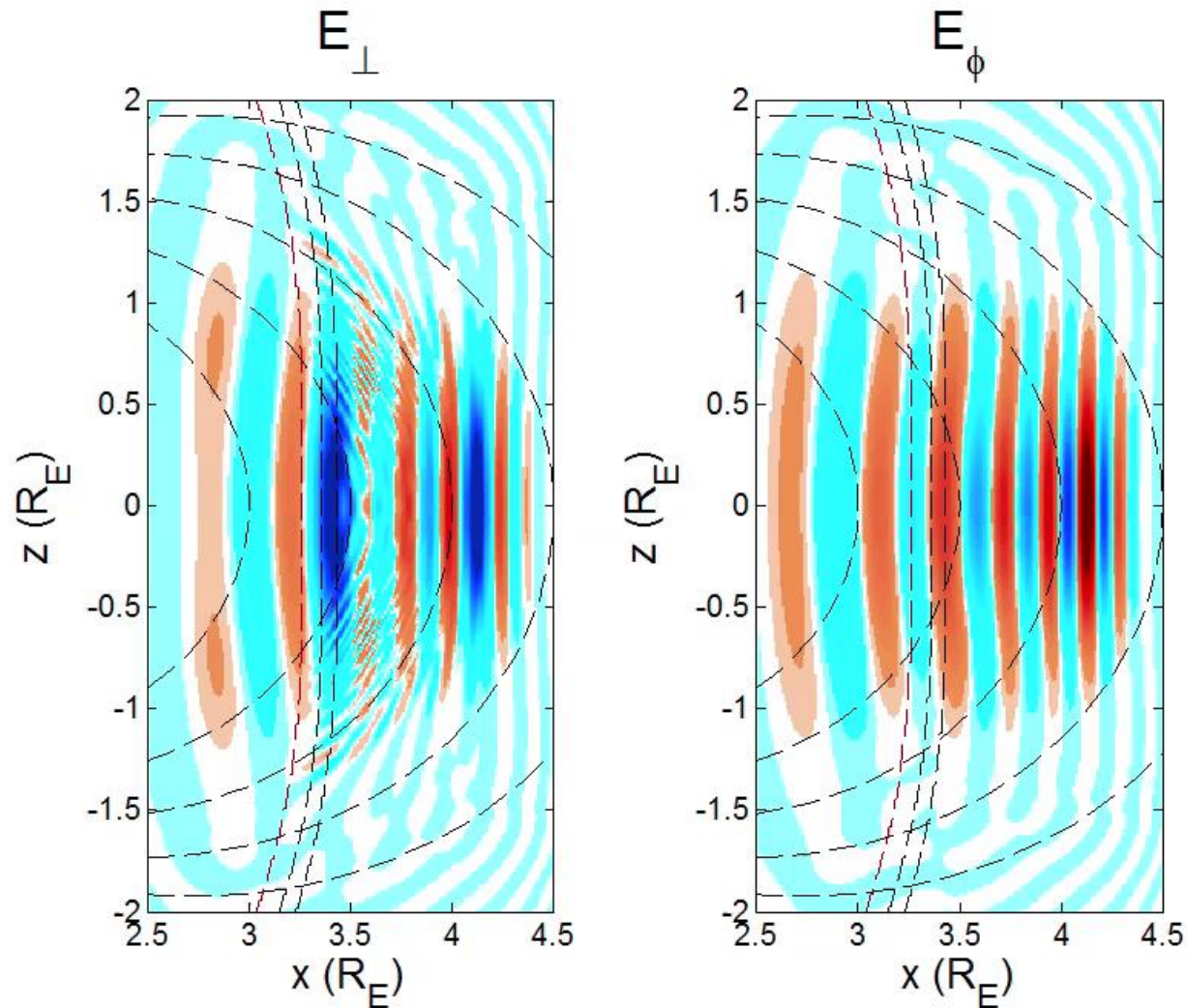
Full wave calculations at Earth

: Mode converted waves \rightarrow linearly polarization

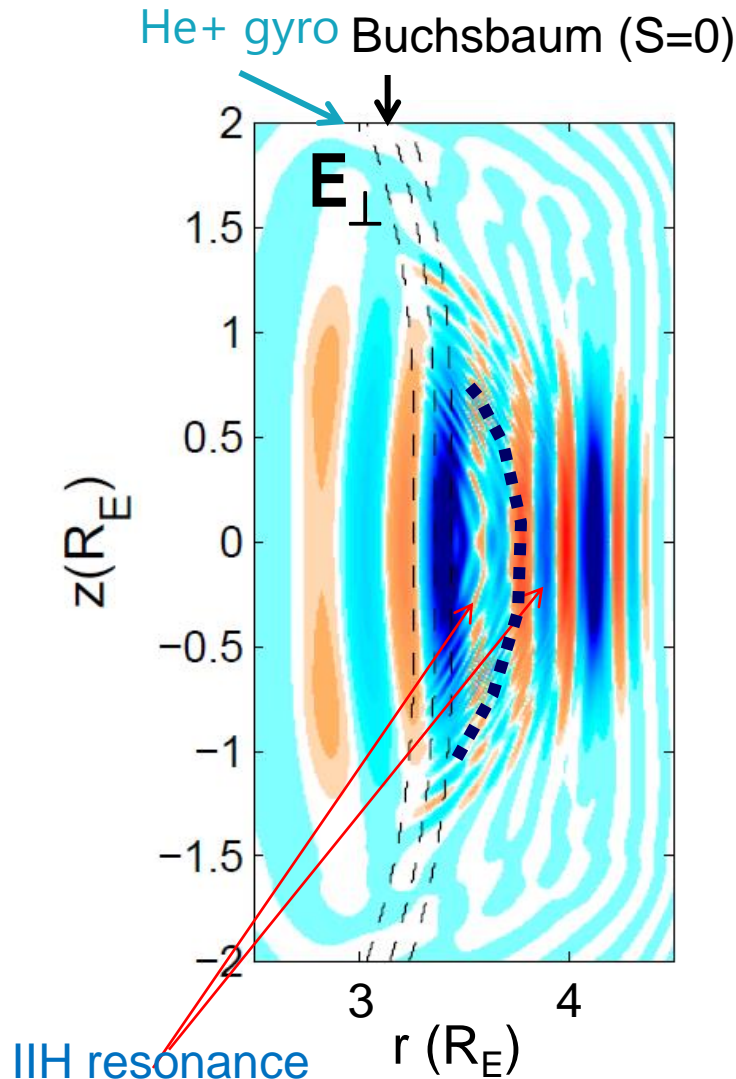
$$f = f_{\text{cHe}} \quad \text{Buchsbaum} \quad L = 0$$



Mode converted waves \rightarrow linearly polarization



Mode converted waves → linearly polarization → **localized**

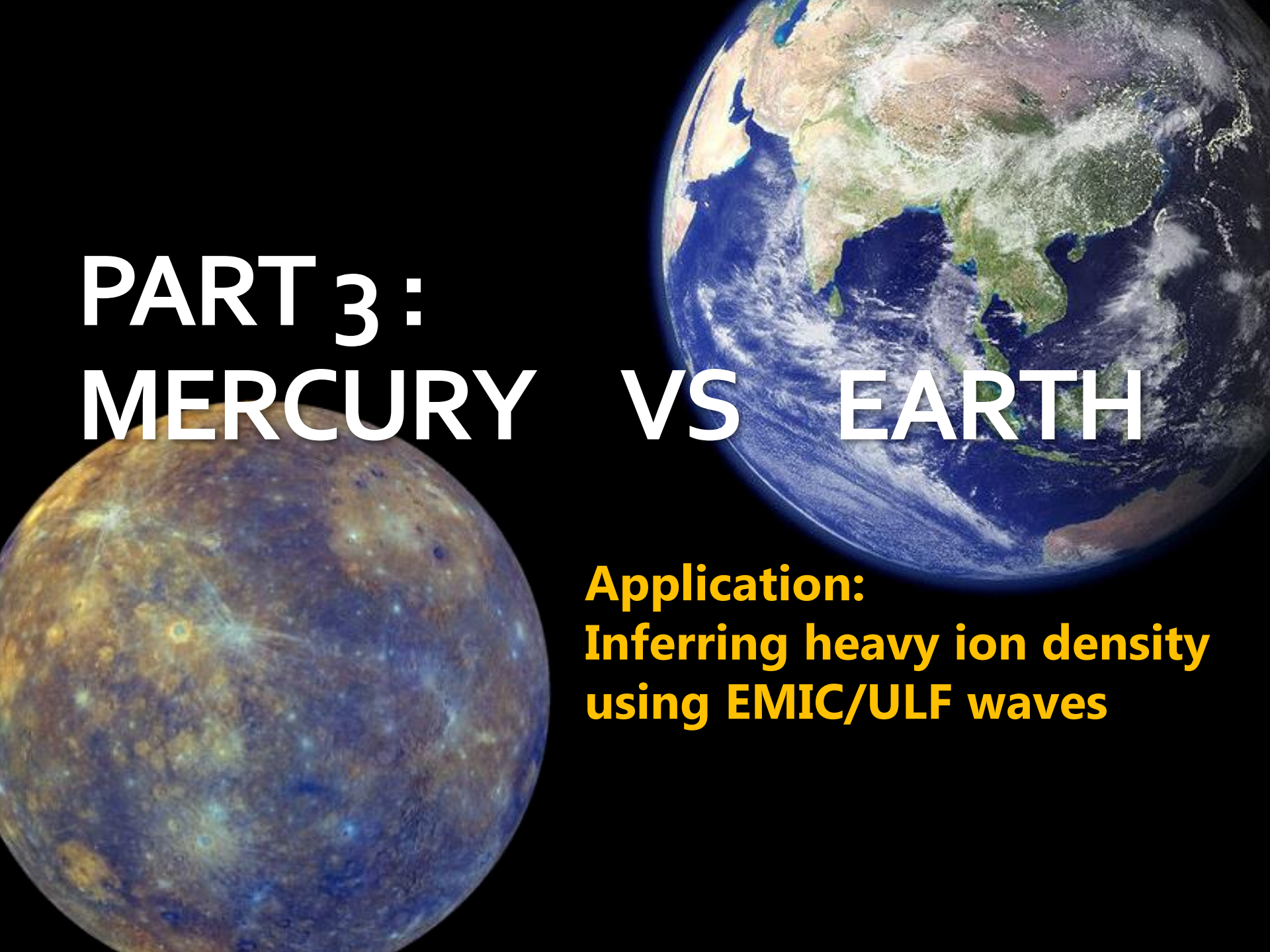


- $f_{\text{He}^+} < f < f_{\text{H}^+}$
- Wave Dispersion
 $n_{\parallel}^2 = S$
- Cut offs occur at $S = 0$
(Buchsbaum resonance)
- IIH resonances are
localized between two
Buchsbaum resonances

[e.g., Johnson et al.,

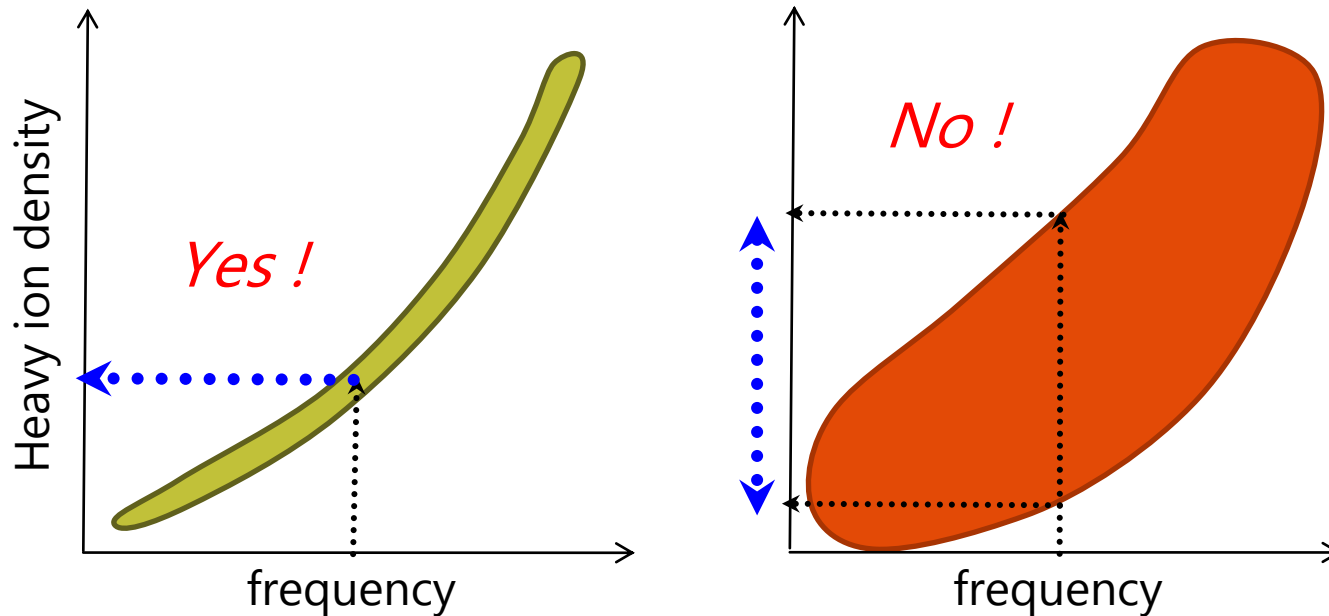
PART 3: MERCURY VS EARTH

**Application:
Inferring heavy ion density
using EMIC/ULF waves**



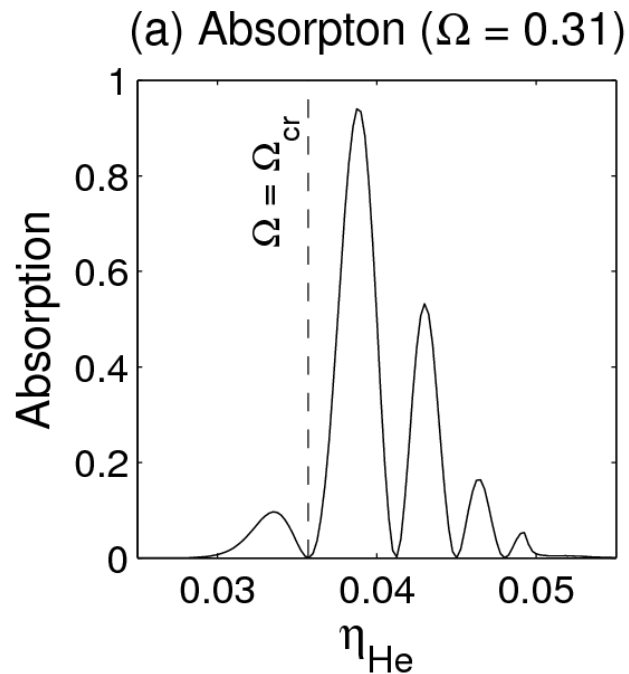
Can detected ULF waves be a diagnostic tool to estimate heavy ion density ratio?

Absorption of fast compressional waves
= Generation of linear polarization waves

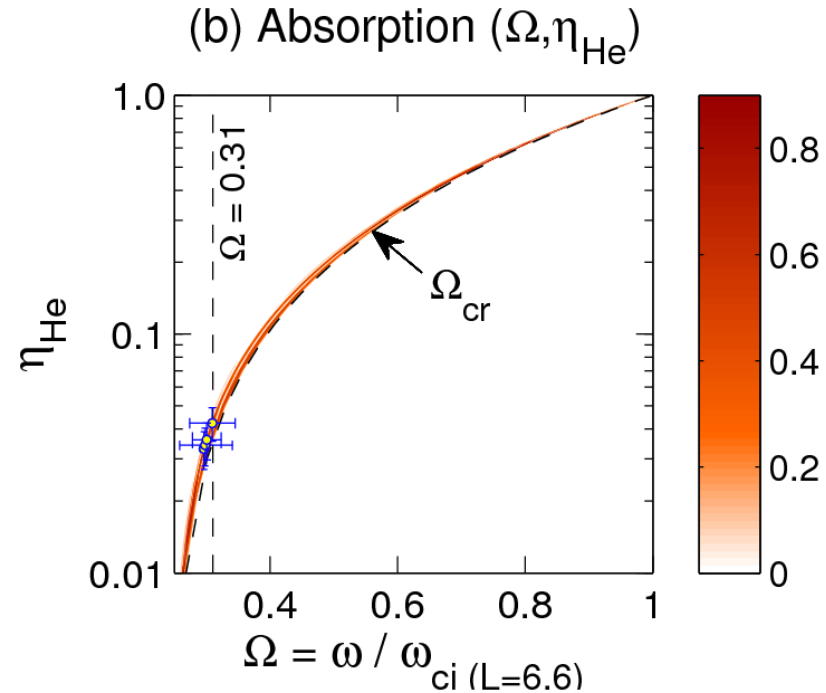


Key point : *width*

Wave absorption at Earth : adopting simple density model



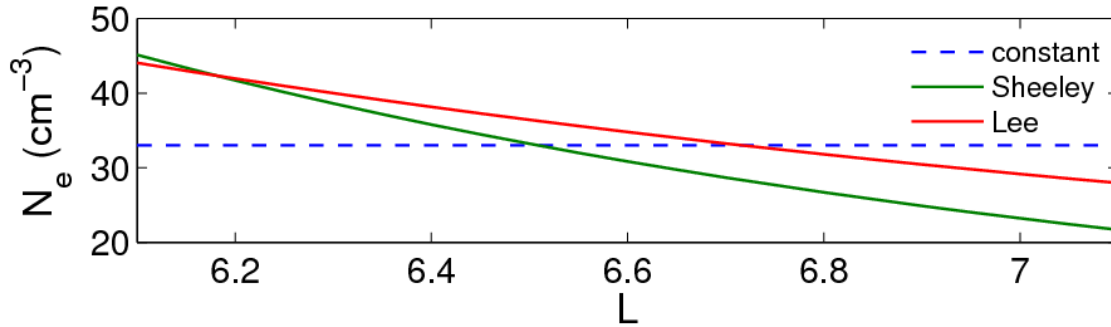
$\Delta\eta_{He} \sim 2\%$



IIH resonance frequency
~ crossover frequency

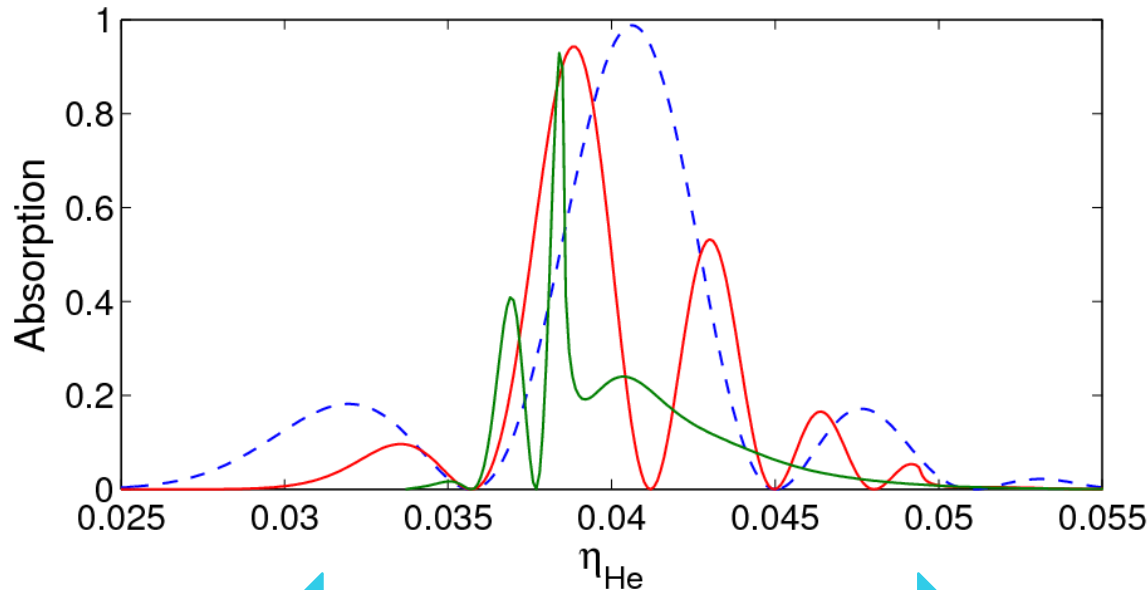
Wave absorption **at Earth** : adopting *various* density model

(a) Electron Density Model

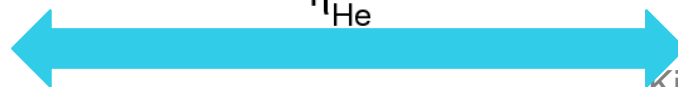


$\Delta\eta_{\text{He}}$: **not sensitive** to the radial structure of electron density profile

(b) $L=6.6$

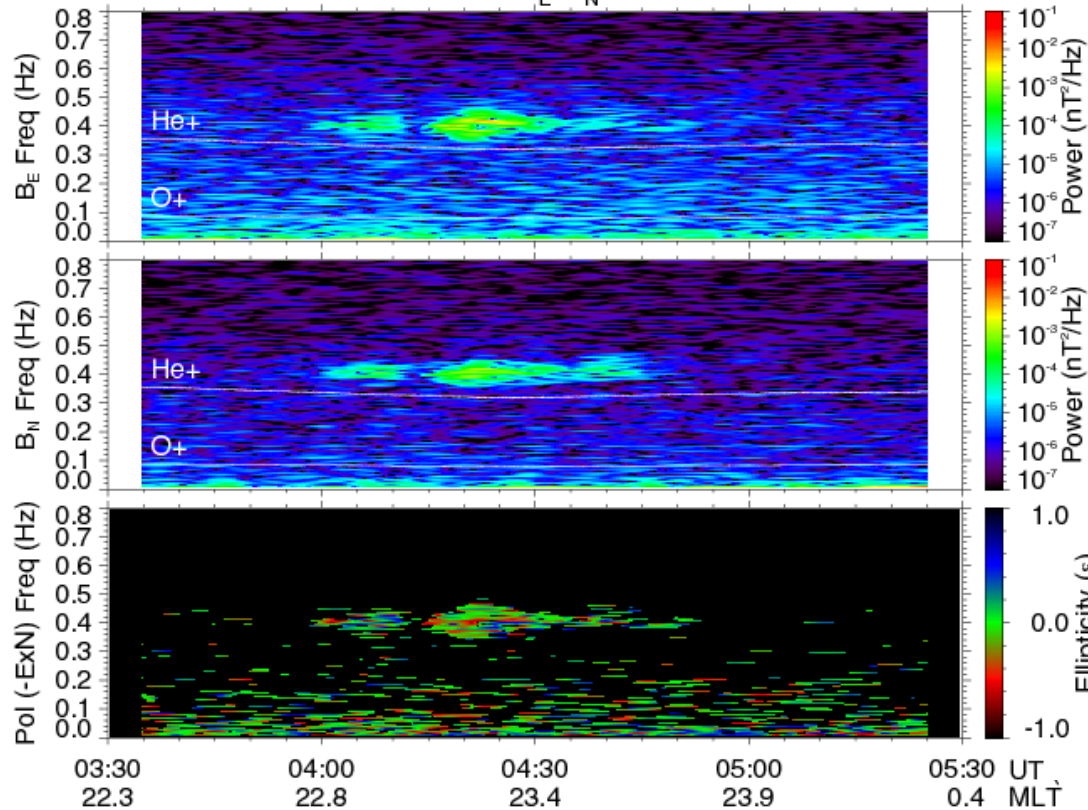


→ η_{He} can be inferred from the observed EMIC waves at **geosynchronous orbit**, which is robust for typical magnetospheric parameters.



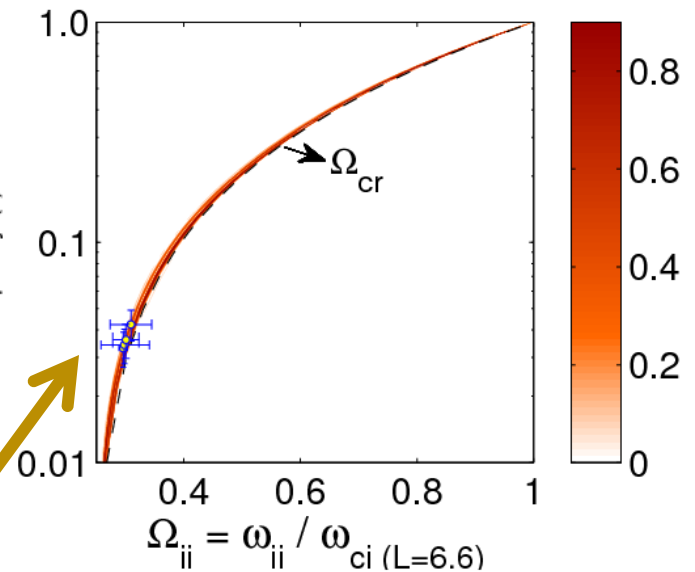
Heavy Ion Density Estimation **at Earth** : Geosynchronous orbit $L \sim 6.6$

GOES-12 FGM $B_E B_N$ Jan/01/2007



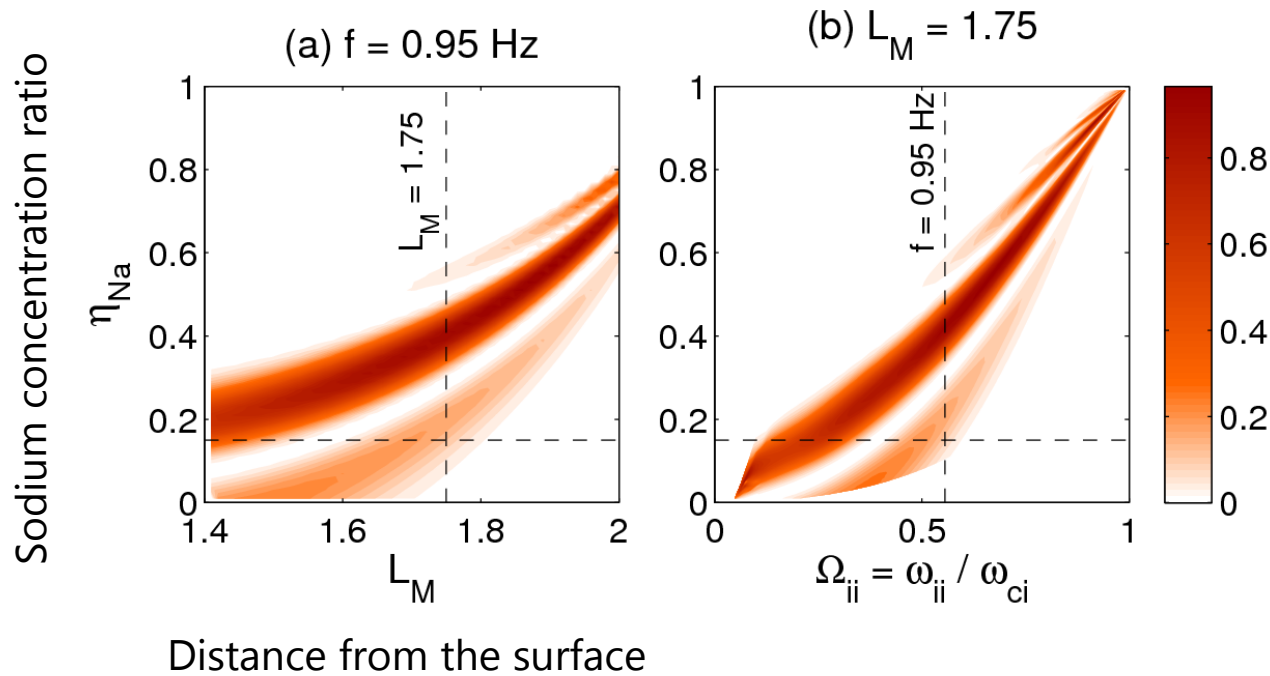
$f \sim 0.35 - 0.45 \text{ Hz}$
 $f / f_{ci} \sim 0.28 - 0.29$

(b) $A(\Omega_{ii}, \eta_{\text{He}})$



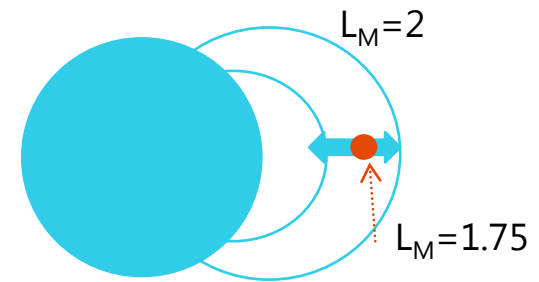
He+ density ratio : $3.3 - 4.2 \pm 0.7 \%$

Wave absorption **at Mercury** : adopting simple density model



$\Delta\eta_{\text{Na}} \sim 40\% !$

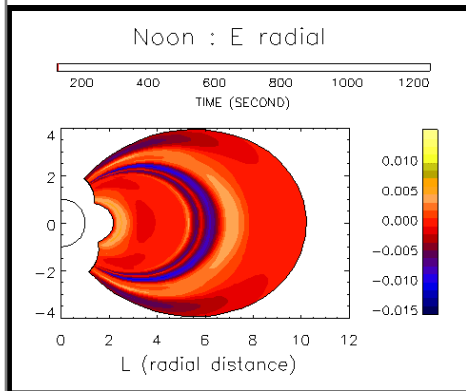
η_{ion} can **NOT** be simply inferred from the observed ULF waves at Mercury



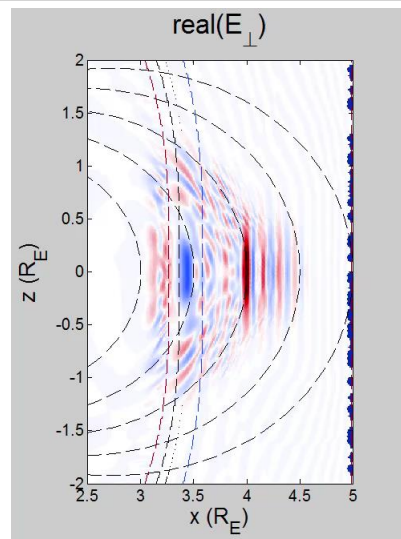
Mode converted waves
at the IIH or Alfvén resonance

Field-aligned Propagation
Linear Polarization

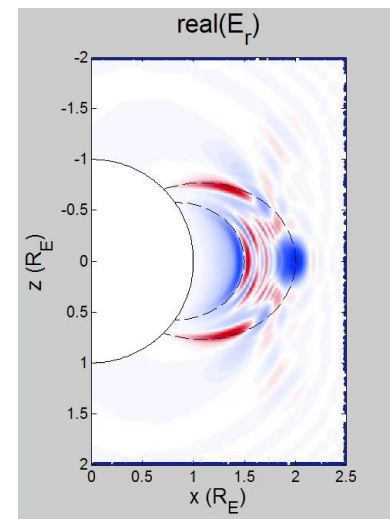
FLR resonance at Earth
(Alfvén resonance : global)



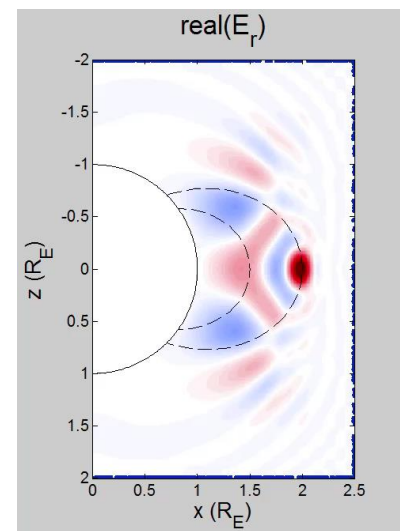
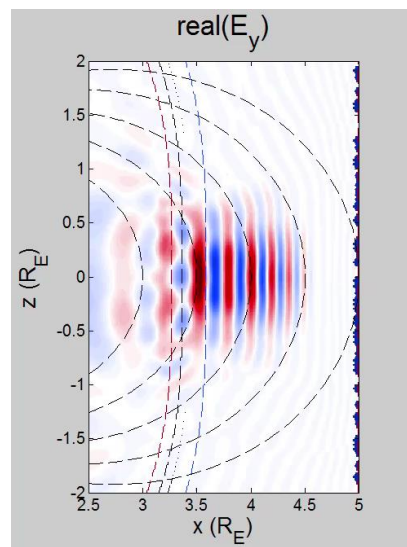
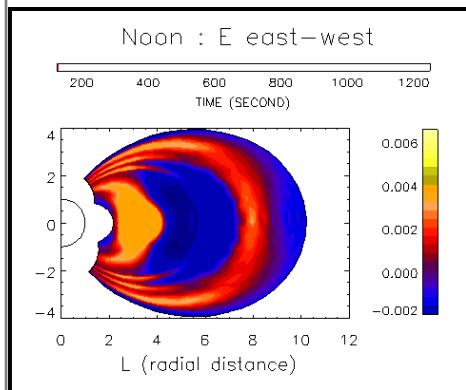
EMIC waves at Earth
(IIH resonance : localized)



FLR at Mercury
(IIH resonance : global)



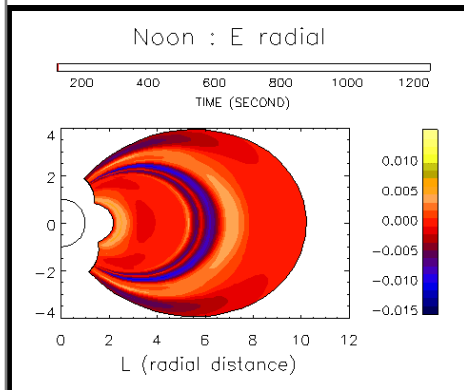
Fast compressional mode
(externally driven incoming waves)



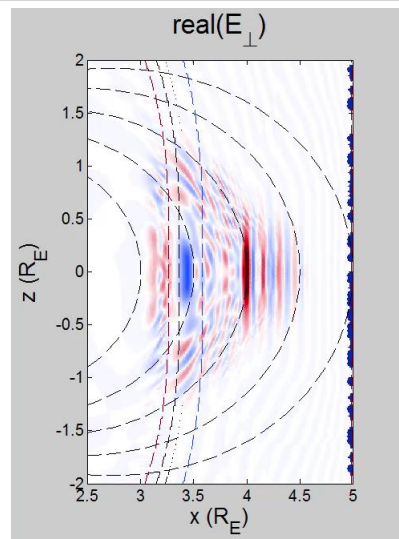
Mode converted waves
at the IIH or Alfvén resonance

Field-aligned Propagation
Linear Polarization

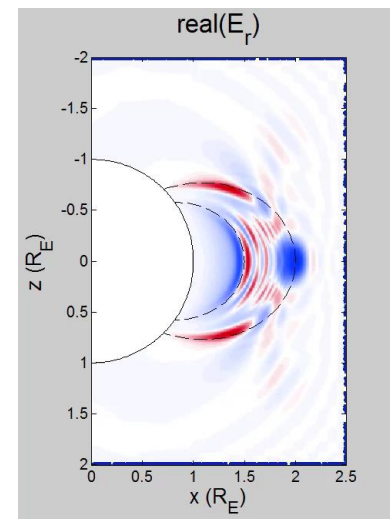
FLR resonance at Earth
(Alfvén resonance : global)



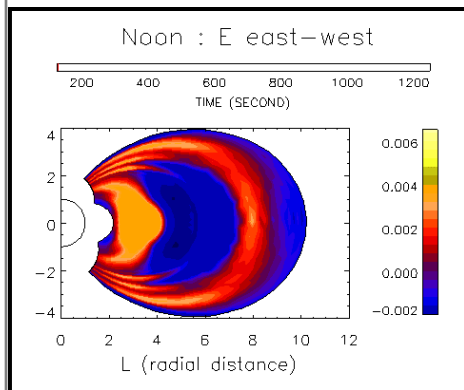
EMIC waves at Earth
(IIH resonance : localized)



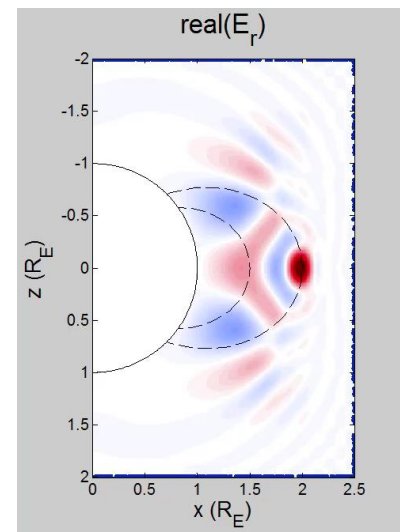
FLR at Mercury
(IIH resonance : global)



Fast compressional mode
(externally driven incoming waves)



Inferring Heavy
Ion Density!



END

Observed linear polarized EMIC waves (IIH resonance) can be used to infer the heavy ion density.

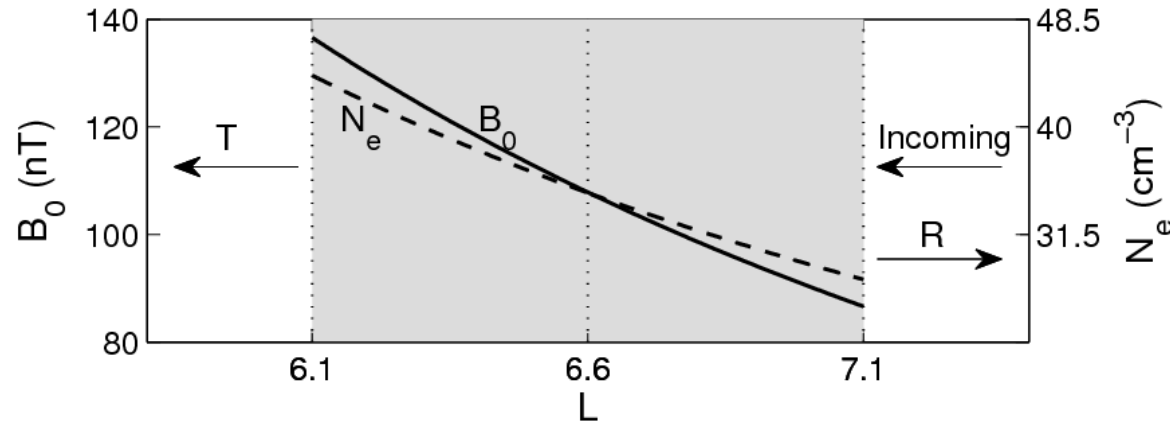
Fast mode **absorption** at the IIH resonance depends on wave frequency ω , azimuthal (k_y), field-aligned wave numbers (k_{\parallel}), heavy ion density ratio, and \mathbf{B}_0 .

→ IIH resonance has been suggested to **estimate heavy ion density** [Kim et al., 2008, Lee et al., 2008]

→ The **sharply peaked dependence of mode conversion on ω** with observed \mathbf{B}_0 makes it possible to **estimate heavy ion density ratio** from the detected EMIC waves

[Kazakov and Fulop, 2013]

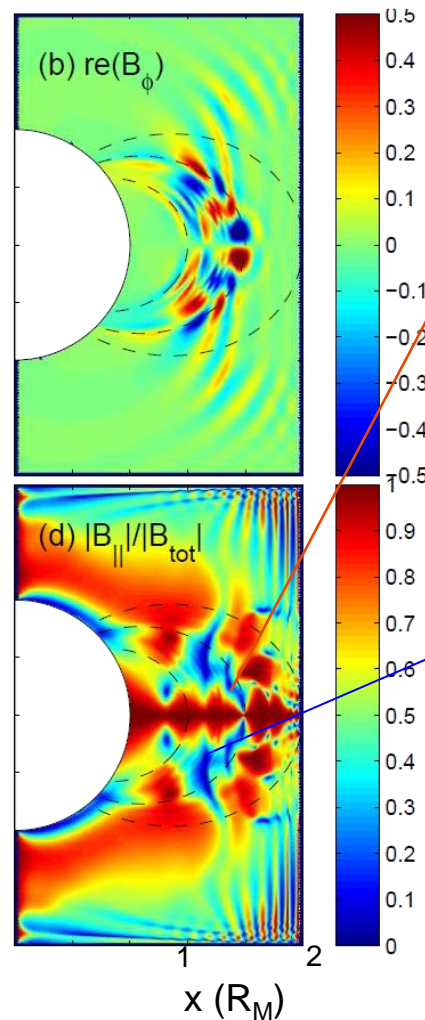
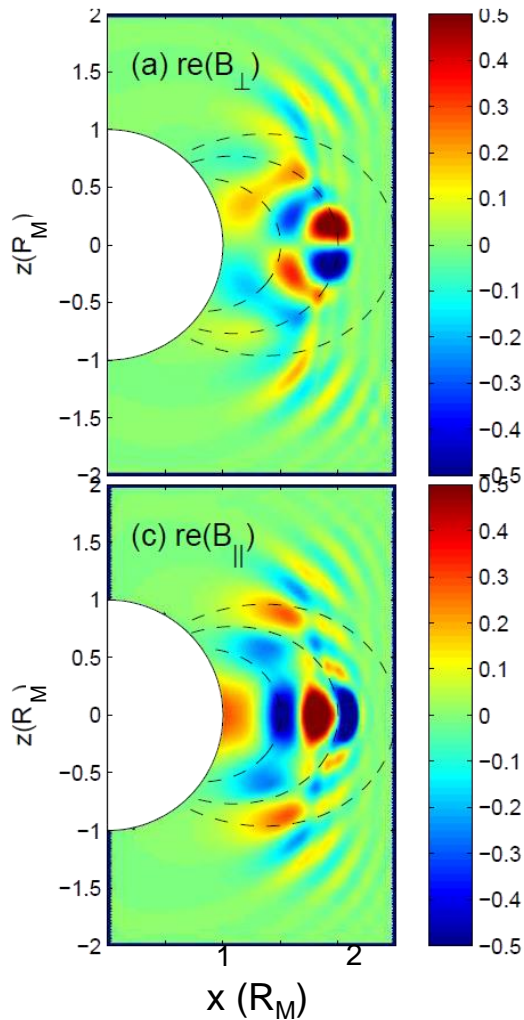
Wave absorption for variable concentration of **He⁺** and ω in dipole field line at **Earth (L=6.6)** are performed



Absorption

Compressibility

$$\delta b_{\parallel} / \delta b$$



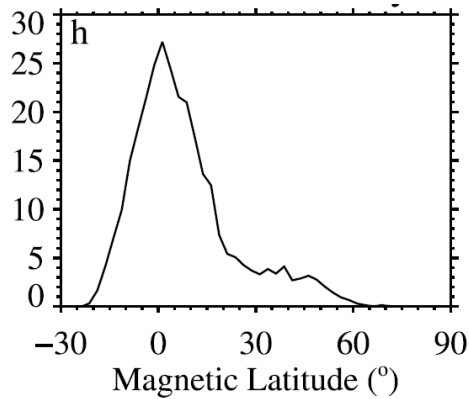
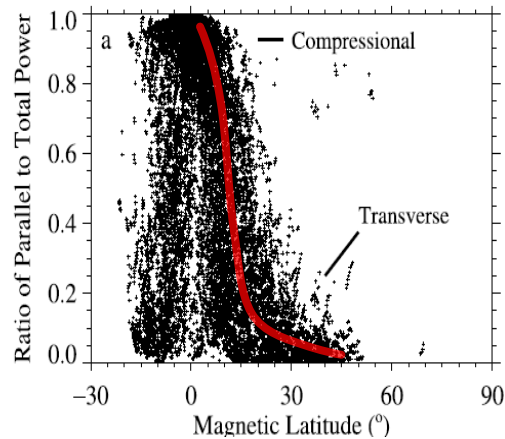
EQUATOR

Compressional component
is dominant
: fast mode
+
field-line resonance

OFF EQUATOR

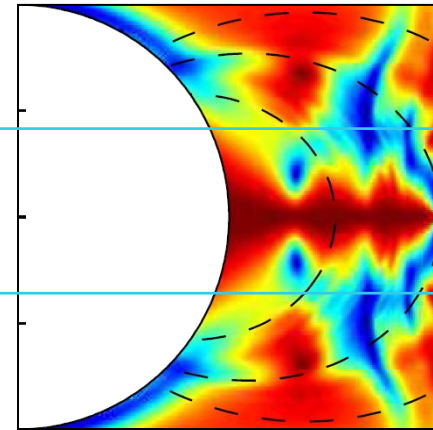
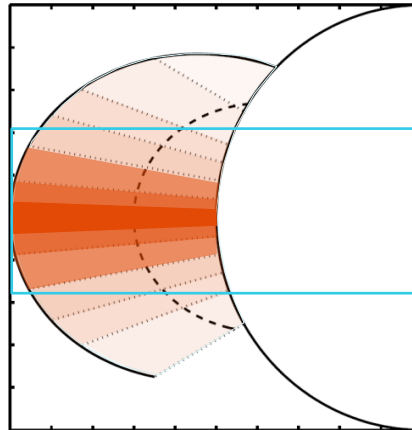
Transverse component
is dominant
: field-line resonance

Comparison with observation



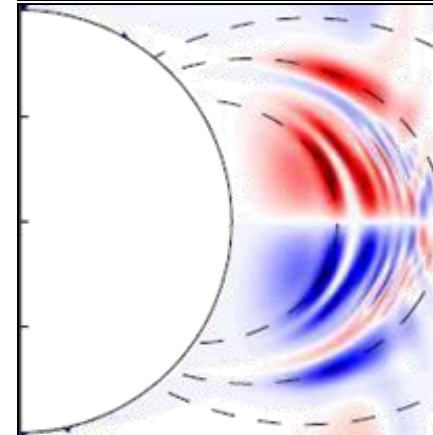
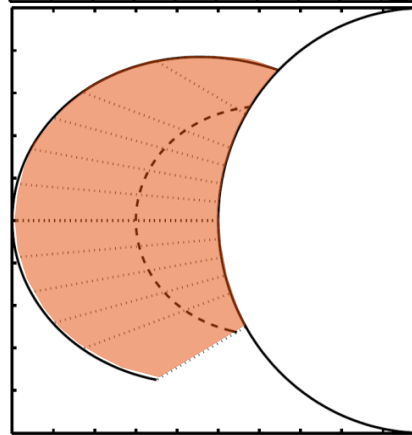
Observation

Full wave calculation



Compressibility

Equator - high
Off Equator - low



Latitude
coverage

Summary 1 : Mercury

1. Reproduce ULF waves at Mercury

- Full wave model
 - Mode conversion from incoming compressional waves to ion-ion hybrid resonance waves
- Ray tracing – Ion Bernstein waves

2. Both wave calculations shows

- Magnetic compressional component is dominant near magnetic equator
- Magnetic transverse component is dominant off equator

3. Which is correct? Long wavelength or short wavelength?

- Several wave modes can be existed, such as short wave length IBW and long wavelength mode-converted waves